# Parsing

Notes on Decomposition

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## 1 Decomposition of Feature Bundles

Given a lexical entry $\mathtt{w} :: \alpha$, we can divide $\alpha$ up into the following parts:

- the part that occurs *before* the first category feature $\mathtt{x}$
- the first category feature itself $\mathtt{x}$
- the part that occurs *after* the first category feature

In a useful lexical item (i.e. one which can be used in a convergent derivation), there will be exactly one category feature, the precategorial part will consist of some number of positive merge and move features ($\mathtt{=x}, \mathtt{x=}, \mathtt{+x}, \oplus\mathtt{x}$), and the postcategorial part will consist of some number of negative move features ($\mathtt{-x}$).

So let again $\mathrm{w} = \mathtt{w} :: \alpha\beta\mathtt{x}\gamma$ be a lexical item with $\alpha\beta$ the precategorial part of its feature bundle (one or both of $\alpha$ and $\beta$ may be empty). We can *decompose* w into two lexical items in the following way (I assume that $\mathtt{w}$ is *fresh*; i.e. no other lexical item has a feature of that type):

| $\mathtt{w} :: \alpha\mathtt{w}$ | $\epsilon :: \mathtt{=w}\beta\mathtt{x}\gamma$ |
|---|---|

From a linguistic perspective, this amounts to saying that what we used to think of as an $XP$ (remember that w had category $\mathtt{x}$) is really *two* phrases, $XP$ with complement $WP$. We can view this process in terms of the trees we would construct in figure 1.

**Exercises** Decompose the following lexical items at the vertical bar

1. $\epsilon :: \mathtt{=V\ +k} \mid \mathtt{d=\ v}$
2. $\mathtt{give} :: \mathtt{=d\ +k} \mid \mathtt{d=\ V}$

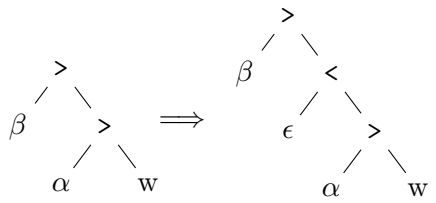



Figure 1: Decomposition in pictures

### 1.1 Decomposition and Generalization

The entire point about this sort of lexical decomposition can be summarized in the following way:

> lexical decomposition allows us to express regularities in the lexicon as new lexical items

If we measure the size of a grammatical description in terms of the number of features used (i.e. the sum of all features on all lexical items), then lexical decomposition can be used to reduce the size of our lexicon, by reifying repeated feature sequences as separate lexical items. Consider the set of lexical items in figure 2. Each of these six lexical items has three features,

| | |
|---|---|
| will : : =v.+k.s | must : : =v.+k.s |
| had : : =perf.+k.s | was : : =prog.+k.s |
| has : : =perf.+k.s | is : : =prog.+k.s |

Figure 2: Some tensed auxiliaries

giving us a total lexical size of 18. However, all six lexical items end with the same length two sequence of features: `+k.s`. This expresses that they check the case of a subject, and are a sentence; in even more naïve terms each lexical item demands that the subject moves to its specifier. We can decompose our lexical items so as to factor this common feature sequence out, giving rise to the lexicon in figure 3. This lexicon has *seven* lexical

| | |
|---|---|
| will : : =v.t | must : : =v.t |
| had : : =perf.t | was : : =prog.t |
| has : : =perf.t | is : : =prog.t |
| $\epsilon$ : : =t.+k.s | |

Figure 3: Some tensed auxiliaries, with some redundancies factored out

items, but only fifteen features. We can see that decomposition has *reified* the repeated feature sequence as a new lexical item, which expresses the generalization that subjects move to a specifier position at (or above) TP (called AgrSP in the literature).

**Exercises**

1. Identify and decompose redundancies in the following set of lexical items.

| | |
|---|---|
| John : : d.-k | Mary : : d.-k |
| the : : =n.d.-k | every : : =n.d.-k |
| no : : =n.d.-k | some : : =n.d.-k |

2. Give a preliminary analysis of the Saxon genitive construction in English (NP's N):
   - John's doctor
   - every man's mother

   Crucially, the NP to the left of the *'s* cannot undergo movement.

## 1.2 Decomposition and Lexical Rules

We have spoken about decomposition in terms of reducing redundancy in our analyses, and alluded to the fact that this seems to capture generalizations about regularities in our lexicon. A more common way of doing this latter is to write *lexical (redundancy) rules*. The 'true' lexicon then is obtained by applying the lexical rules (repeatedly) to the lexical items one has. As an example, we might consider an instance of the VP-topicalization construction:

- Laugh, John will.

We might analyze this as containing the following dependencies: The lexical items corresponding to this dependency structure are given below. We notice that the *will* participating in the VP topicalization construction differs from our previously analyzed *will* in that its feature bundle has an additional `+top` feature immediately before the category feature. Similarly, the *laugh* participating in this construction differs from *laugh* elsewhere in having an additional `-top` feature immediately after its categorial feature. This situation is not particular to *will* and *laugh*, but is common to all topicalization hosts and topicalizers respectively. We might decide to account for this lexical regularity by means of a rule, which states that we may add a

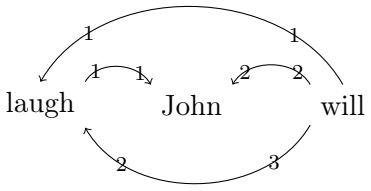



Figure 4: Dependencies for sentence *Laugh, John will*

John :: d.-k  will :: =v.+k.+top.s
laugh :: =d.v.-top

Figure 5: Lexical items extracted from the dependency structure in figure 4

+top feature to any lexical item with feature bundle ending in s immediately before this feature, and one which states that we may add a -top feature to the end of any lexical item's feature bundle ending in v, as shown in figure 6. Then we only need to have our familiar, non-topicalizing lexical items in our lexicon, the others being obtainable from these via these two rules.

We can also use our decomposition operation on the doubled lexical items, as their feature bundles overlap significantly with already extant lexical items. Decomposing laugh :: =d | v.-top at the mark between the features =d and v, we obtain our familiar *laugh* lexical item, alongside a silent lexical item: $\epsilon$ :: =v.v.-top.[1] Doing the same to will :: =v.+k | +top.s, we obtain, next to our familiar *will*, the silent lexical item $\epsilon$ :: =s.+top.s.

These new, silent, lexical items allow us to, during the course of a syntactic derivation, add a -top feature to the end of any lexical item ending with the feature v, and a +top feature right before the s feature of any lexical item with category s. In short, these silent lexical items behave just as do the lexical rules in figure 6.

[1]Our decomposition operation allows us to pick any category to connect the two new lexical items. We have chosen v, so as to make one of the new lexical items identical to our old *laugh*.

**Rule 1** if w :: $\alpha$.s is a lexical item, then so is w :: $\alpha$.+top.s

**Rule 2** if w :: $\alpha$.v is a lexical item, then so is w :: $\alpha$.v.-top

Figure 6: lexical rules

is : : =prog.+k.s  been : : =prog.perf

Figure 7: Various forms of (auxiliary) *be*

### 1.3 Decomposition and Syntactic Word-Formation

Our decomposition scheme as described above treats the two parts of lexical items (their phonological and syntactic forms) asymmetrically; the syntactic feature sequence is split, but the phonological segment sequence is not. We can imagine, however, wanting to factor out redundancy, not only within feature bundles, but within the *relation* between phonological forms and feature bundles. Consider the pair of lexical items in figure 7. Not only do both of these lexical items begin with an =prog feature, but (we know) they are all forms of the auxiliary verb *be*. This generalization is, however, not expressed in the language of our theory (i.e. in terms of our lexicon). We would like to *factor out* the auxiliary from its endings. Abstractly, we need a decomposition rule like the following:

$$\mathsf{w} : : \alpha\beta \mapsto \begin{cases} \mathsf{u} : : \alpha.\mathsf{x} \\ \mathsf{v} : : \underline{=\mathsf{x}}.\beta \\ w = u \oplus v \end{cases}$$

This rule would allow us to split a lexical item into two, but now the original phonological form of the lexical item ($w$) is factored into two pieces ($u$ and $v$). The resulting pair of lexical items no longer give us the same structures we would have created with the original one, as now there are two heads (a $u$ and a $v$) instead of just one ($w$), and in addition all specifiers in $\alpha$ intervene between these two heads. In order to remedy this problem, we must allow $u$ and $v$ to combine to form $w$. We do this in two steps. First, when merging expressions headed by $u$ and $v$ respectively, we combine the phonological material from both heads, and put them together into just one of the two.[2] Second, we record that these two heads are not pronounced separately as $u$ and $v$, but are rather pronounced together as $w$. This is done in two ways. First, in the lexical entry for $v$ (the selector), we record (by underlining the relevant feature) that it enters into a special relationship with the head of its selected argument (=x). Second, we record that $u$

[2] Just which head should host the phonological material is something we shall address in a bit.

```
s :: =v.+k.s     en :: =v.perf
be :: =prog.v
```

$$is = be \oplus s$$
$$been = be \oplus en$$

Figure 8: Factoring out /be/

and $v$ are jointly pronounced as $w$.[3] This latter is, in linguistic theory, the provenance of morphology. It is simply represented here as a finite list of statements (morphology can be thought of as a way of compressing this list, or alternatively a way of identifying and expressing rule-like generalizations). Using this decomposition rule, we obtain the lexical items in figure 8.

### 1.4 Complex heads

Once we move from whole word syntax to one which manipulates sub-word parts,[4] we must confront two questions.

1. how do the heads which constitute a single word get identified?
2. where does the word corresponding to multiple distinct heads get pronounced?

The answer to the first question we gave implicitly in the previous section: two heads are part of the same word just in case one selects for the other with an underlined feature. There are many possible answers to the second question. Following Brody [2000], we say that a word is pronounced (relative to other words) as though it occupied the position of the highest of its heads (with respect to c-command) with a particular property (and in the lowest of its heads, if none have that property). This property is called *strength* in Brody's work, but is formally merely an *ad hoc* property of lexical items. To distinguish between strong and weak lexical items, we write strong lexical items with three colons separating their phonological and syntactic features, and weak ones with the usual two (as in figure 9).

[3] It would make sense as well to, upon combining $u$ and $v$, to replace them with $w$. I prefer, when doing theory construction, to factor out logically distinct steps: syntax will then assemble complex heads, and these complex heads will be interpreted elsewhere. Of course, when actually **using** this theory to model performance, these logically distinct steps can and perhaps should be interleaved with one another.

[4] In current parlance, this would be described as moving from a pre-syntactic morphological module to a post-syntactic one.

$\mathsf{u} :: \alpha \quad \mathsf{v} :: \beta$

Figure 9: Strong (left) and weak (right) lexical items

## 2 Decomposition and Learning

Decomposition can be thought of as a part of a *learning* mechanism for minimalist grammars. In particular, it provides a principled route from a whole-word syntactic analysis to the sort of decompositional syntactic analysis which is characteristic of minimalist-style analyses.

It is known that learning can take place in minimalist grammars in a highly supervised setting [Kobele et al., 2002, Stabler et al., 2003], where

1. words are segmented into morphemes
2. ordered and directed dependencies link words which are in a feature checking relationship
   - the $i^{th}$ dependency of word $u$ connects it to the $j^{th}$ dependency of word $v$ just in case the $i^{th}$ feature of word $u$ was checked by the $j^{th}$ feature of word $v$
   - the source of the dependency is the attractor feature, and the target of the dependency is the attractee feature

In this setting, the learner is given (essentially) full lexical items where feature names are unique to a particular dependency, and the learner's task is to identify which feature distinctions should be kept, and which should be collapsed. In the cited works (following Kanazawa [1998]), the pressure to collapse distinctions is provided by a limit on the number of homophones in the grammar.

We can use our decomposition mechanism to relax the supervision provided by the segmentation of words into morphemes (1). Accordingly, we assume that we are provided with sentences based on whole words, with dependency links between them as described by point 2 above.

### 2.1 English auxiliaries

As a simple case study, consider the English auxiliary system. Imagine the learner being exposed to sentences like the following.

1. John eats.

2. John will eat.

3. John has eaten.

4. John will have eaten.

5. John is eating.

6. John will be eating.

7. John has been eating.

8. John will have been eating.

The dependencies for sentence 8 are as in 10. From these dependencies,

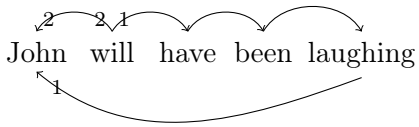



Figure 10: Dependencies for sentence 8

we can reconstruct the lexical items in figure 11. Here, the names of the features are arbitrary. After extracting lexical items from sentences 1 – 8,

| | |
|---|---|
| John : : a.-b | will : : =c.+b.s |
| have : : =d.c | been : : =e.d |
| laughing : : =a.e | |

Figure 11: Lexical items extracted from the dependency structure in figure 10

we have multiple 'copies' of certain words, which differ only in the names (but not the types) of features in their feature bundles. For example, there are eight (!) different copies of *John*, four of *eating*, three of *will*, and two each of *eaten*, *has*, and *been*. We can unify these copies into single lexical items by renaming the features involved across the whole lexicon. For example, we might decide to rename the first feature of each of the *John* lexical items to `d`, which would force us to replace all features with name `a` with the name `d`, among others. After this unification procedure, we are left with the lexicon on figure 12.

This grammar is perfectly capable of deriving the sentences (with the appropriate dependencies) we were given originally. However, it systematically

| | |
|---|---|
| John :: d.-k | eats :: =d.+k.s |
| will :: =v.+k.s | eat :: =d.v |
| has :: =perf.+k.s | eaten :: =d.perf |
| is :: =prog.+k.s | eating :: =d.prog |
| have :: =perf.v | be :: =prog.v |
| been :: =prog.perf | |

Figure 12: Lexical items after unification of features

*misses* generalizations: although we know (as English speakers) that there is a single verb, *eat*, which is appearing in its various forms in this lexicon, this fact is not captured in the grammar. Although this feels right, it is a somewhat wishy-washy argument. A more concrete (although less intuitively appealing) argument to the effect that there are missed generalizations, is that in order to add a new verb to our grammar we would need to add *four* separate lexical items (six, if we had included the past tense and the passive voice), one for each cell in its (derivational) paradigm.

We thus want to express generalizations about our language in terms of our theory, and this we will do via decomposition. There are many ways to begin; we want to compare pairwise lexical items to one another which have similar prefixes/suffixes and (ideally) similar phonologies. We should then decompose, and unify, decompose, and unify, until further decomposition does not achieve any succinctness gains. However we will here simply note *en masse* that the *eat* verbs begin with *eat*, and with the feature =d, and decompose them. The result is shown in figure 13 Note that the original

| | |
|---|---|
| John :: d.-k | s :: =V.+k.s |
| will :: =v.+k.s | $\epsilon$ :: =V.v |
| has :: =perf.+k.s | en :: =V.perf |
| is :: =prog.+k.s | ing :: =V.prog |
| have :: =perf.v | be :: =prog.v |
| been :: =prog.perf | eat :: =d.V |
| | |
| $eats = eat \oplus s$ | $eaten = eat \oplus en$ |
| $eating = eat \oplus ing$ | $eat = eat \oplus \epsilon$ |

Figure 13: Lexical items after decomposition of *eat*

bare *eat* form has also been decomposed, leaving behind a 'dummy' lexical item which serves to simply change category. This is important, so that no new forms are derived: decomposition does not change the language of the

grammar.

In the next step, we do the same with the forms of *be*.[5] This is shown in figure 14. There are three as yet unjustified moves just made:

| | |
|---|---|
| John :: d.-k | s :: =V.+k.s |
| will :: =v.+k.s | $\epsilon$ :: =V.v |
| has :: =perf.+k.s | en :: =V.perf |
| s :: =x.+k.s | ing :: =V.prog |
| have :: =perf.v | $\epsilon$ :: =x.v |
| en :: =x.perf | eat :: =d.V |
| | be :: =prog.x |

| | |
|---|---|
| $eats = eat \oplus s$ | $eaten = eat \oplus en$ |
| $eating = eat \oplus ing$ | $eat = eat \oplus \epsilon$ |
| $been = be \oplus en$ | $be = be \oplus \epsilon$ |
| $is = be \oplus s$ | |

Figure 14: Lexical items after decomposition of *be*

1. the two $\epsilon$ forms are unifiable, but have not been
2. the two *en* forms are unifiable, but have not been
3. the two *s* forms are unifiable, but have not been

Regarding the first, the $\epsilon$ forms serve solely to assert so-called **isa** relationships between categories (every expression of type V *is an* expression of type v). These must not be unified, as their presence preserves the syntactic distinctions present in the input sentences.[6] There are three basic possibilities for dealing with the two *en* forms:

1. unify V and x
2. assert that V **isa** x
3. assert that x **isa** V

[5] There is a deep issue here, regarding how we are to know that *is* is a form of *be*. There has been computational work on identifying morphological paradigms [Lee, 2014], which might very well be of use here.

[6] They can be replaced by partial ordering statements of the form $V \leq v$ and $x \leq v$ (see Szabolcsi and Bernardi [2008]).

Pursuing options 1 or 3 would collapse necessary syntactic distinctions, leading the grammar to generate sentences of the form: *John will be (being)*$^*$ *eating*. The correct option is 2. This can be determined in a less intuitive manner by identifying cycles in selection (or the lack thereof) in the lexicon: a `V` can be turned into a `prog` (via *ing*), which can be turned into an `x` (via *be*), but an `x` cannot become a `V`. The same reasoning applies to the two *s* forms. Adding this information (as an empty lexical item) to our lexicon gives us the lexicon in figure 15.

| | |
|---|---|
| John :: d.-k | |
| will :: =v.+k.s | $\epsilon$ :: =V.x |
| has :: =perf.+k.s | |
| s :: =x.+k.s | ing :: =V.prog |
| have :: =perf.v | $\epsilon$ :: =x.v |
| en :: =x.perf | eat :: =d.V |
| | be :: =prog.x |

| | |
|---|---|
| $eats = eat \oplus s$ | $eaten = eat \oplus en$ |
| $eating = eat \oplus ing$ | $eat = eat \oplus \epsilon$ |
| $been = be \oplus en$ | $be = be \oplus \epsilon$ |
| $is = be \oplus s$ | |

Figure 15: Lexical items after asserting that `V` **isa** `x`

We turn now to *have*, which results in the lexicon in figure 16. Again,

| | |
|---|---|
| John :: d.-k | |
| will :: =v.+k.s | $\epsilon$ :: =V.x |
| s :: =y.+k.s | |
| s :: =x.+k.s | ing :: =V.prog |
| $\epsilon$ :: =y.v | $\epsilon$ :: =x.v |
| en :: =x.perf | eat :: =d.V |
| have :: =perf.y | be :: =prog.x |

| | |
|---|---|
| $eats = eat \oplus s$ | $eaten = eat \oplus en$ |
| $eating = eat \oplus ing$ | $eat = eat \oplus \epsilon$ |
| $been = be \oplus en$ | $be = be \oplus \epsilon$ |
| $is = be \oplus s$ | $has = have \oplus s$ |
| $have = have \oplus \epsilon$ | |

Figure 16: Lexical items after decomposing *have*

decomposition has given rise to two unifiable instances of the morpheme *s*. There are the same three options, and searching for the patterns of connectivity in the lexicon between `y` and `x` demonstrate that `x` can become a `y` (via the route *be–en–have*) but `y` cannot become an `x`. Thus we assume that `x` **isa** `y`, as is shown in figure 17.

| | |
|---|---|
| John :: d.-k | |
| will :: =v.+k.s | $\epsilon$ :: =V.x |
| s :: =y.+k.s | |
| $\epsilon$ :: =x.y | ing :: =V.prog |
| $\epsilon$ :: =y.v | |
| en :: =x.perf | eat :: =d.V |
| have :: =perf.y | be :: =prog.x |
| | |
| $eats = eat \oplus s$ | $eaten = eat \oplus en$ |
| $eating = eat \oplus ing$ | $eat = eat \oplus \epsilon$ |
| $been = be \oplus en$ | $be = be \oplus \epsilon$ |
| $is = be \oplus s$ | $has = have \oplus s$ |
| $have = have \oplus \epsilon$ | |

Figure 17: Lexical items after asserting that `x` **isa** `y`

This lexicon has 24 features in it (18, if we discount the **isa** lexical items), whereas the initial lexicon (prior to decomposition) contained 26 features. We have thus achieved a (small) compression. However, the important difference between these two lexica lies in their behaviour as more words are added to them; open class words such as intransitive verbs contribute just two features to our final lexicon, but 9 features (distributed over four lexical items) to our initial one.

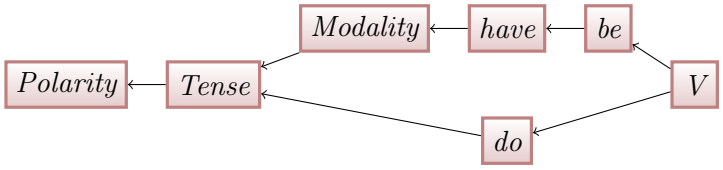
# 3 An Example

## 3.1 English auxiliaries

In analysing the English auxiliary system, we notice a number of coöccurrence restrictions, summarized by the flowchart below.[7] This should be read from right to left (following the arrows), and an arrow from one node X to

[7]Here we are taking the position that modals may combine with tense, thereby viewing elements like *could*, *would*, etc as *can* + *d* and *will* + *d* respectively. Note then that *will* is really *will* + *s*!

another Y should be read as 'an X may be selected by a Y'. For example, a verb (V) may be selected for either by the auxiliary *be* or by *do*. In the former case, we might continue with *have*, but in the latter, we must move on directly to tense (T).




We give a lexicon for the English auxiliary system in figure 18, as well as a flowchart-like hypergraph representation of the lexicon, below.[8] In the hypergraph, the nodes are categories (technically, negative polarity features), and the hyperedges represent lexical items. This hypergraph represents the lexicon, which is intended to *implement* (or account for) the empirical observations summarized intuitively with the flowchart above. In the flowchart, it was neglected to mention that, for example, when *be* selects for the verb, the verb appears in a progressive form (V-ing). This however must be implemented in the lexicon, and is depicted in the hypergraph by having the lexical item *ing* combine with the verb, and only then the lexical item *be*. The hypergraph also makes explicit that this is optional, by means of the silent lexical item taking us from the `v` category directly to the `z` category, skipping over the *ing* and the *be*.

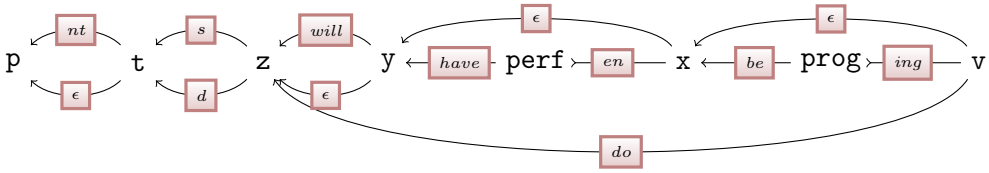



Figure 18 describes in addition the syntactic heads which are interpreted as part of the same morphological word, but has not expressed how these morphological words are to be interpreted. By itself, the syntactic analysis will overgenerate (in conjunction with lexical entries for verbs, arguments, and argument surface positions), allowing us to generate as a cluster of heads forming a morphological word something which we would expect to be a

[8] Left out of the lexicon is the head $\epsilon$ `::: =p.+k.s` which hosts a subject position.

| | |
|---|---|
| nt ::: =t.p | $\epsilon$ ::: =t.p |
| d ::: =z.t | s ::: =z.t |
| will ::: =y.z | $\epsilon$ ::: =y.z |
| have ::: =perf.y | en ::: =x.perf |
| be ::: =prog.x | ing ::: =v.prog |
| $\epsilon$ ::: =x.y | $\epsilon$ ::: =v.x |

do ::: =v.z

Figure 18: A lexicon for the English auxiliary system

verbal form like *laughsn't* (as *laugh* + $\epsilon$ + $\epsilon$ + $\epsilon$ + *s* + *nt*).[9] There does not seem to be an elegant way of blocking this syntactically given our basic analysis thus far.[10] Still, we may note that all illegitimate forms share the property that the lexical verb is part of a morphological word with a head of category p. To rule out the incorrectly generated sentences, we must add a constraint that this is not allowed.[11] As we have not yet specified the morphological component, we can most simply implement this constraint here. Thus we are forced to claim that it is a morphological fact about English (not a syntactic one) that *laughsn't* (and, more generally, any negative form of a verb) is not a word.

Even with this small lexicon, there are too many possible combinations of heads to make it fun to write them all down individually. Instead, we assign a morphological interpretation to (what are intuitively) our affixes, and adopt implicitly a paradigmatic model of morphology to interpret them. This is depicted in Figure 19. The figure describes which morphological features each 'affix' expresses, and we appeal to a model of morphology which is able to take a stem paired with a number of morphological features and realize it as the appropriate member of that stem's paradigm. Two example paradigms are given in Figure 20. Note that there are no negative forms for

[9]To deal with subject auxiliary inversion, we could add another lexical item, which triggers head movement of the head of s: $\epsilon$ ::: =s.q. Then we also allow that lexical verbs may be inverted with their subjects: $*$*laughs John*.

[10]Our solution is elegant in that it does not posit unmotivated lexical ambiguity. (One word has one feature bundle.) Although we have multiple silent lexical entries in figure 18, these are all expressing that a particular derivational route is *optional*, and could be eliminated in favor of using *partially ordered categories*. Then we would stipulate that v $\leq$ x $\leq$ y $\leq$ z, and that t $\leq$ p, and allow that anything that has a feature =w may instead select for anything which is less than or equal to w.

[11]There has been much work on the nature of constraints, both in phonology and in syntax. A common theme is that if constraints are *regular*, in that they can be represented as finite state devices, then this does not add to the expressive power of the formalism.

$$
\begin{aligned}
\texttt{nt} :: \texttt{=t.p} &\mapsto \texttt{neg} \\
\epsilon :: \underline{\texttt{=t}}\texttt{.p} &\mapsto \emptyset \\
\texttt{d} :: \underline{\texttt{=z}}\texttt{.t} &\mapsto \texttt{+past} \\
\texttt{s} :: \underline{\texttt{=z}}\texttt{.t} &\mapsto \texttt{-past} \\
\epsilon :: \underline{\texttt{=y}}\texttt{.z} &\mapsto \emptyset \\
\texttt{en} :: \underline{\texttt{=x}}\texttt{.perf} &\mapsto \texttt{perf} \\
\texttt{ing} :: \underline{\texttt{=v}}\texttt{.prog} &\mapsto \texttt{prog} \\
\epsilon :: \underline{\texttt{=x}}\texttt{.y} &\mapsto \emptyset \\
\epsilon :: \underline{\texttt{=v}}\texttt{.x} &\mapsto \emptyset
\end{aligned}
$$

Figure 19: Translating between heads and morphological features

| BE | prog | perf | +past | -past |
|---|---|---|---|---|
| | being | been | was | is |
| neg | - | - | wasn't | isn't |

| LAUGH | prog | perf | +past | +past |
|---|---|---|---|---|
| | laughing | laughed | laughed | laughs |
| neg | - | - | - | - |

Figure 20: Paradigms for *be* and *laugh*

the verb *laugh*. This is where the morphological stipulation occurs, which reins in the otherwise overgenerating syntactic component. Observe as well that there is a lot of regularity in the morphological paradigms, both within and across paradigms. A theory of morphology can be thought of as a device for expressing these regularities.

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