
FIRST-PRINCIPLES MODELLING OF DOPANTS AT INTERFACES IN TCO MATERIALS

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Workshop „Transparente und flexible Elektronik“
Universität Leipzig, 28. September 2010

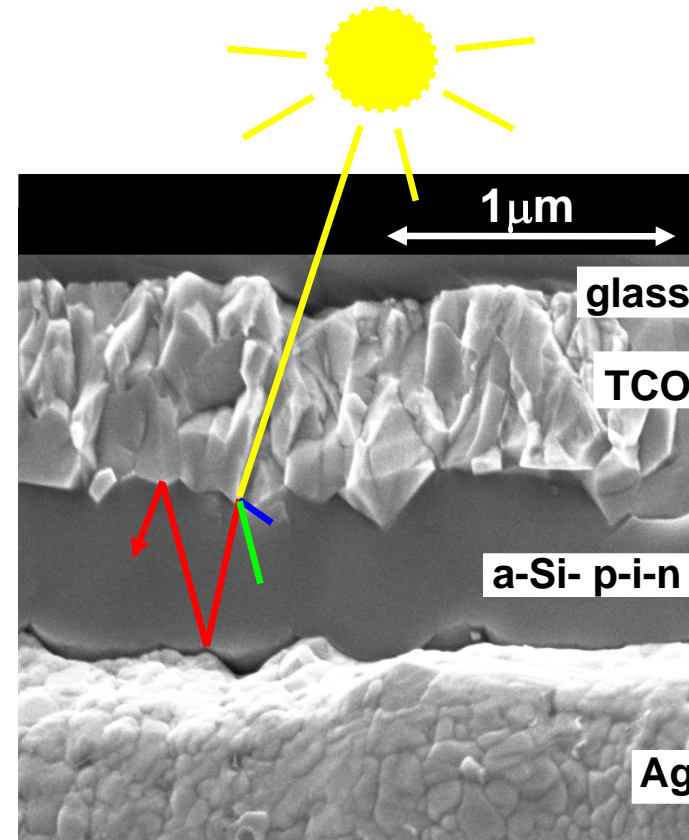
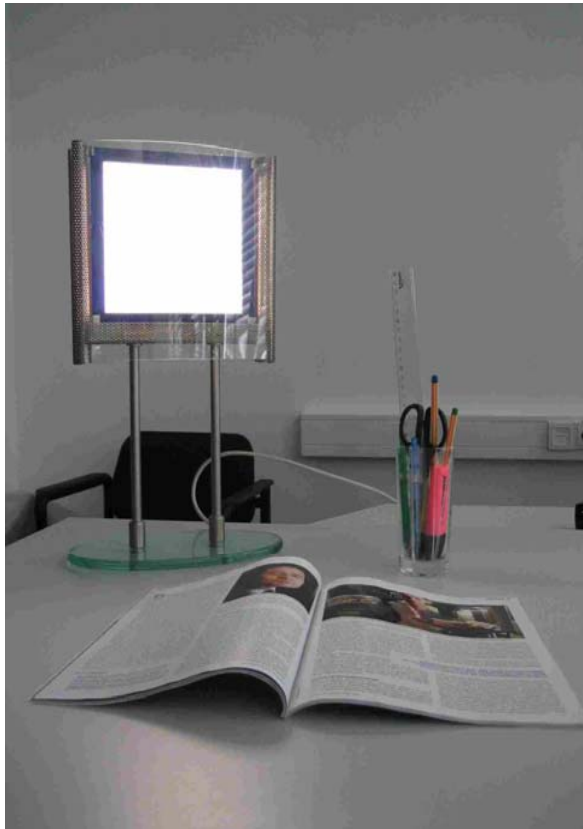
$$\underline{\sigma} = \underline{\sigma}(\underline{\varepsilon})$$

$$m_i \ddot{x}_i = f_i$$

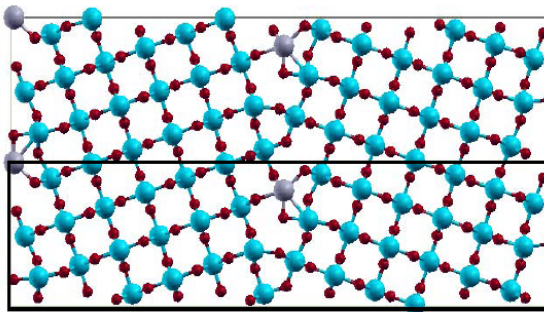
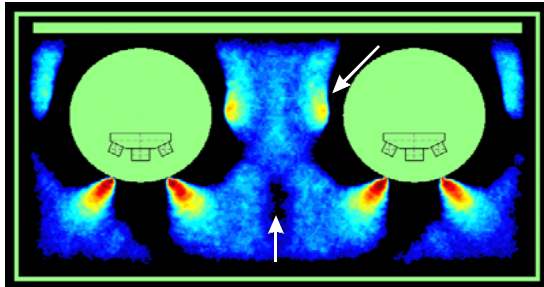
$$\hat{H} \Psi = E \Psi$$

First-principles DFT study of dopant elements at grain boundaries in the TCO materials ZnO and TiO₂

Wolfgang Körner and Christian Elsässer, Fraunhofer IWM



METCO – a Multidisciplinary Effort towards advanced Transparent and Conducting Oxide electrodes

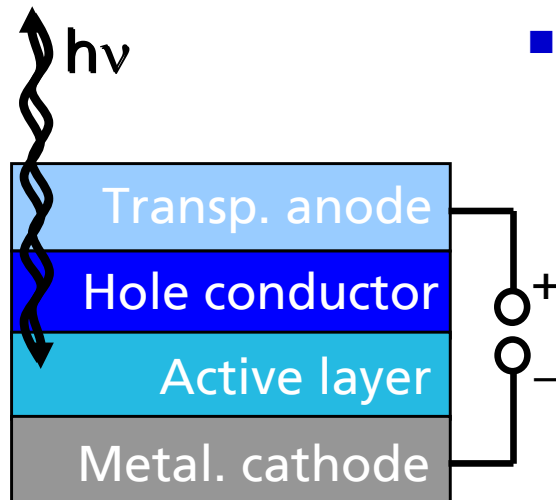


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<http://www.transparente-elektroden.de/>

Transparent and conductive oxide thin-film systems



- need: large-area electrical contacts for solar cells and light emitting diodes
- demands:
 - high optical transmittance and electrical conductance
 - proper matching of band structures at interfaces
 - sufficient light scattering for thin-film solar cells
 - capability for patterning and processing
 - low-cost film deposition on large areas
- desire: p-doping ... p-n hetero-junctions ... transparent electronics

ZnO

- TCO: transparent and conducting oxide **ZnO:X (X = N, P, Al, Ga)**
 - alternative material to ITO
 - large-area thin-film top electrode for solar cells or OLED devices
 - polycrystalline microstructure
 - **interaction of dopants with grain boundaries**
- DFT: density functional theory
 - LDA: local density approximation, for optimisation of atomic structures
 - **formation energies** of structural defects
 - SIC: self interaction correction, for analysis of electronic structures
 - **defect levels** in energy gap of more accurate band structure
 - supercell models, **m**ixed **b**asis, **p**seudopotentials (MBPP code)

First-principles Density Functional Theory

Mixed-basis pseudopotential method

Meyer, Elsässer, Lechermann, Fähnle, et al. (origin: MPI-MF Stuttgart)

density functional theory

LDA, GGA ... SIC-LDA, LDA+U ...

translational lattice symmetry

periodic supercell models

core-valence interactions

norm-conserving pseudopotentials

valence electrons

plane waves and localized orbitals



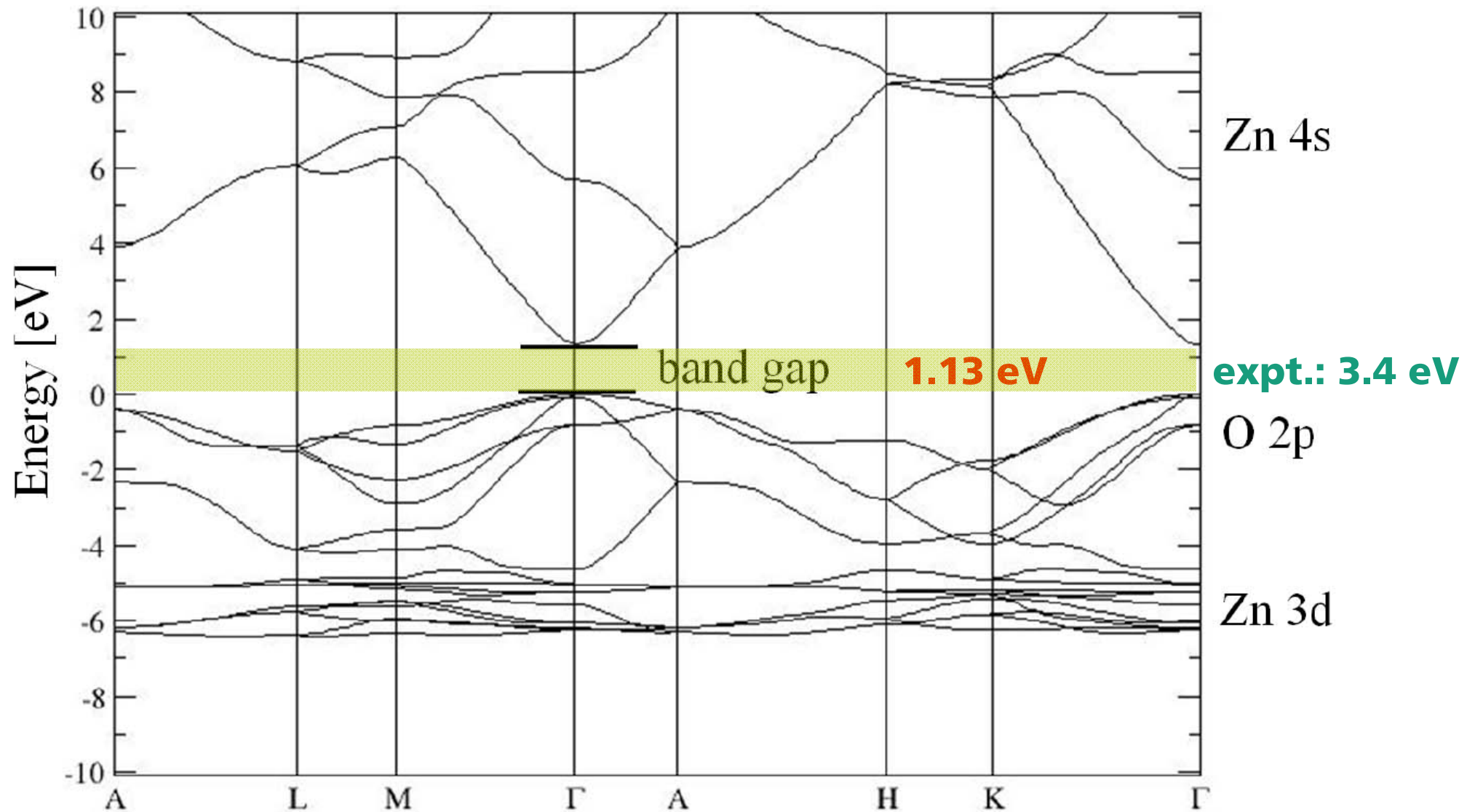
⇒ output: energies and forces

crystal structures, defect configurations

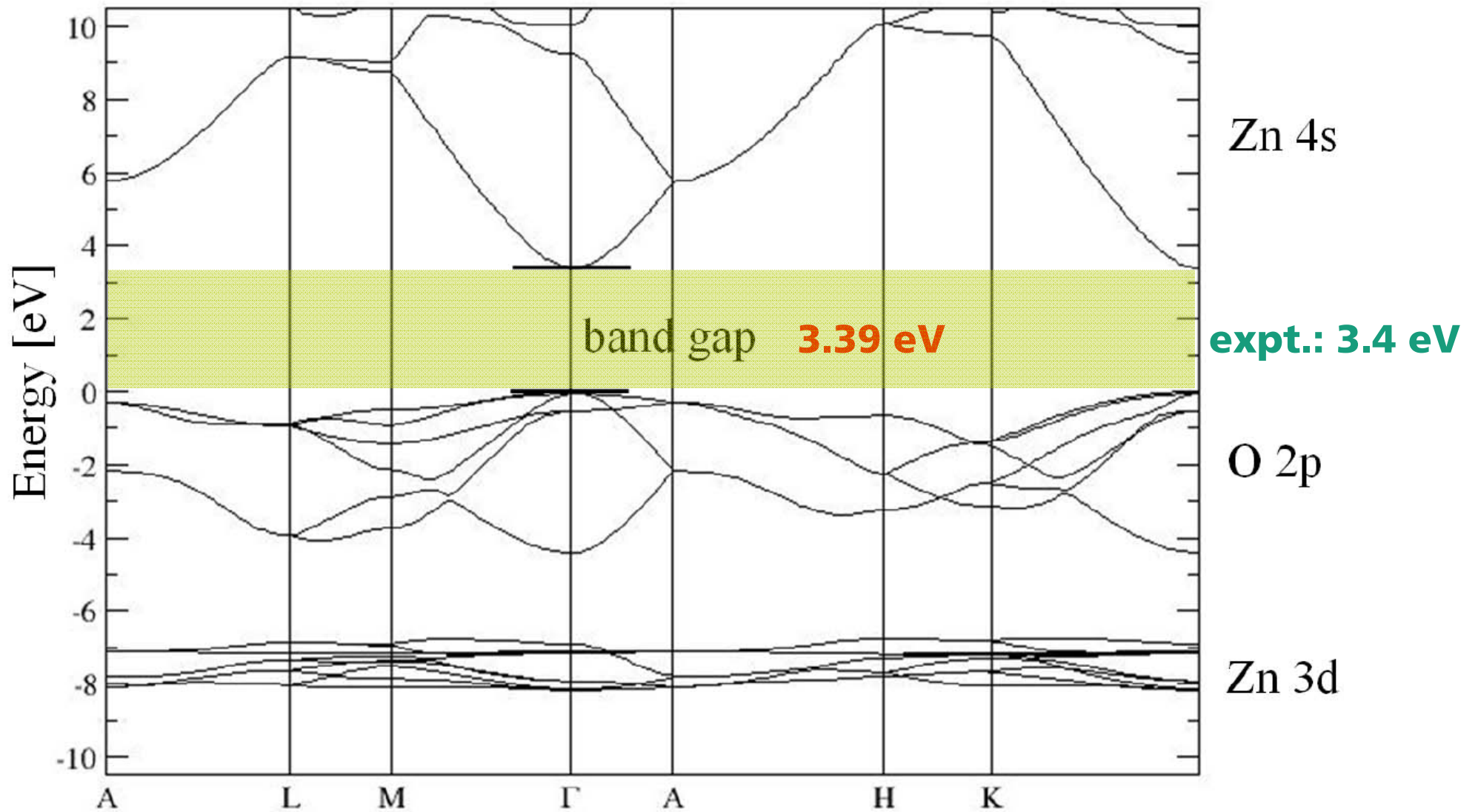
electronic structure, chemical bonding

phase stabilities, defect energies

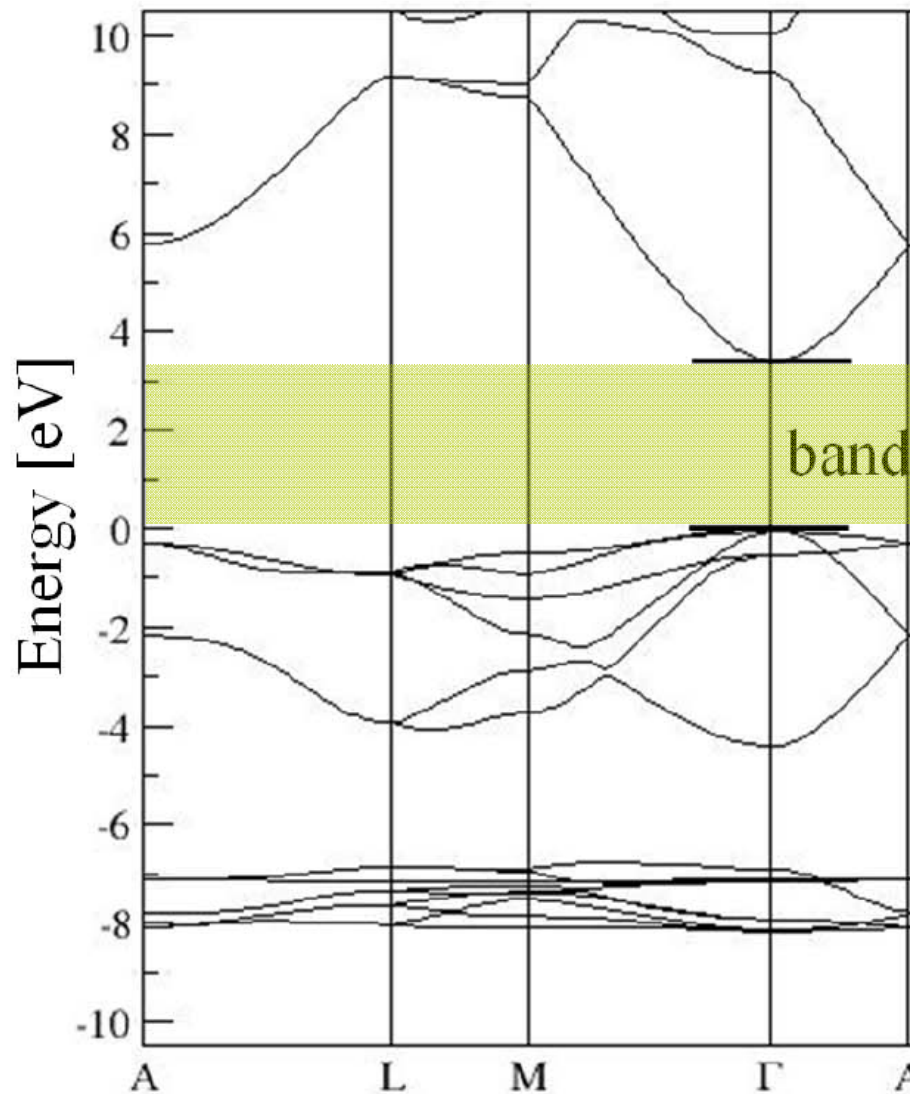
Band structure of bulk ZnO – LDA



Band structure of bulk ZnO – SIC



Band structure of bulk ZnO – SIC



■ formalism: **SIC pseudopotentials**

cf. Vogel, Krüger, Pollmann

Phys. Rev. B 54 (1996) 5495

$$\left(-\nabla^2 + V_l + V_H[n_v] + V_{xc}[n_v] - w_l \underbrace{\left[V_H[n_l] + V_{xc}[n_l] \right]}_{:= -V_{cor}[n_l]} \right) \Psi_l^{pp} = \epsilon_l^{pp} \Psi_l^{pp}$$

$$V_l^{SIC}(r) := V_l(r) - \alpha \langle \Psi_l^{pp}, V_{cor}[n_l] \Psi_l^{pp} \rangle \Psi_l^{pp}(r)$$

■ other SIC PP implementations, e.g.:

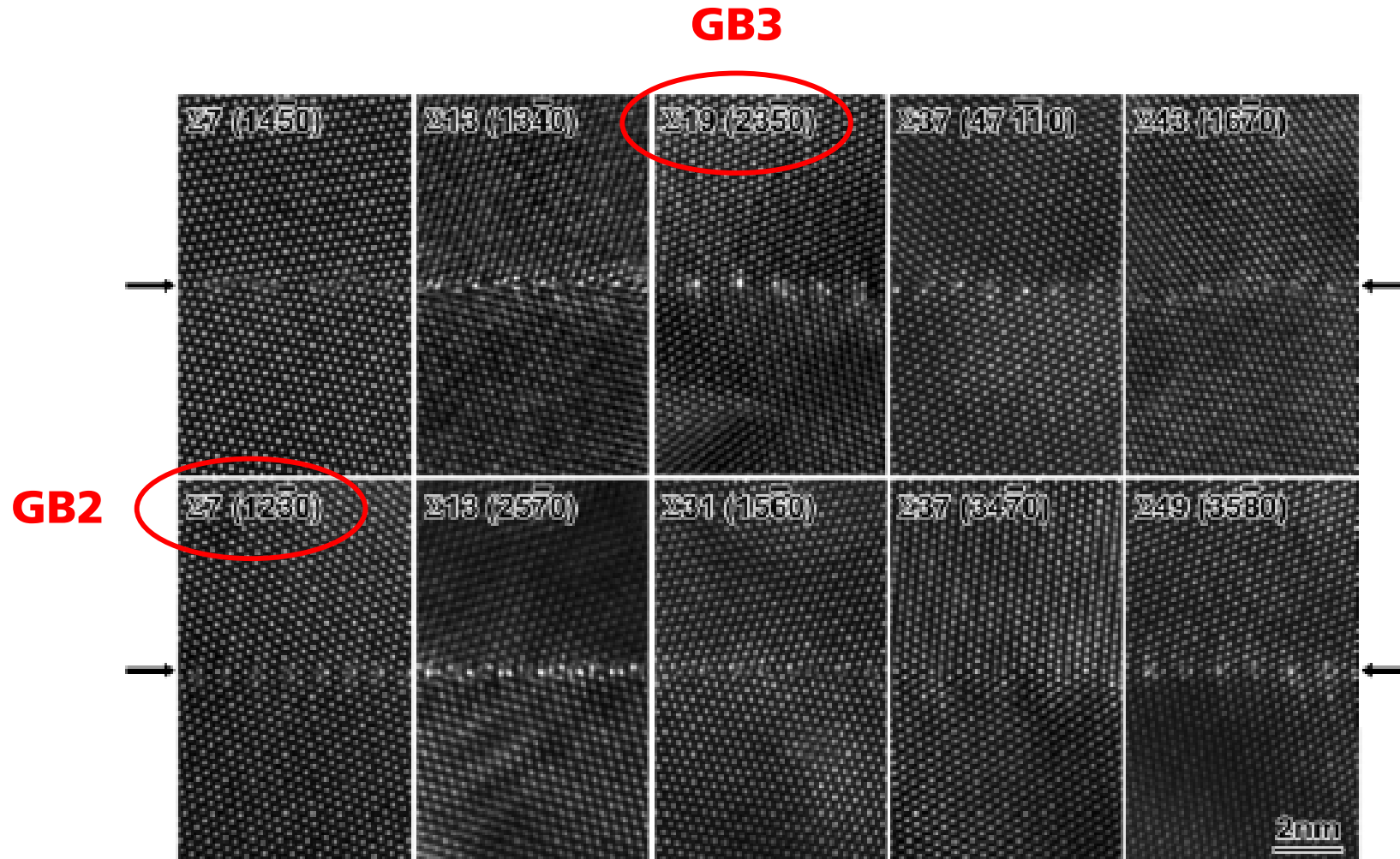
Filippetti and Spaldin

Phys. Rev. B 67 (2003) 125109

Pemmaraju et al.

Phys. Rev. B 75 (2007) 045101

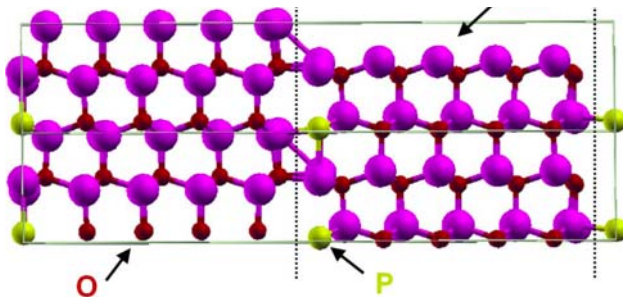
Grain boundaries in ceramic ZnO – bicrystal experiments



Sato et al., J. Am. Ceram. Soc. 90 (2007) 337-357

Supercells for three different GB in ZnO

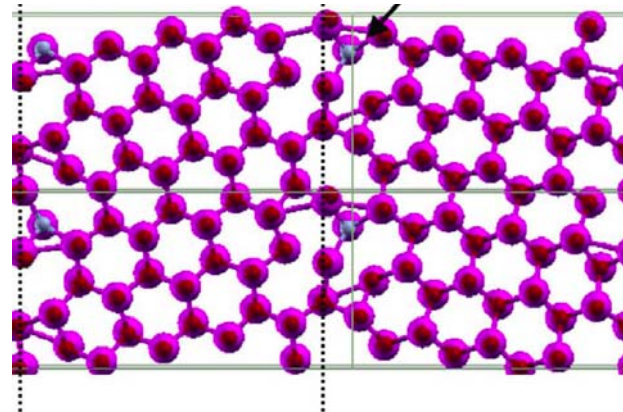
GB1: $(10\bar{1}0)[10\bar{1}0] \Sigma 1$



80 atoms

$$E_{GB1} = 0.17 \text{ J/m}^2$$

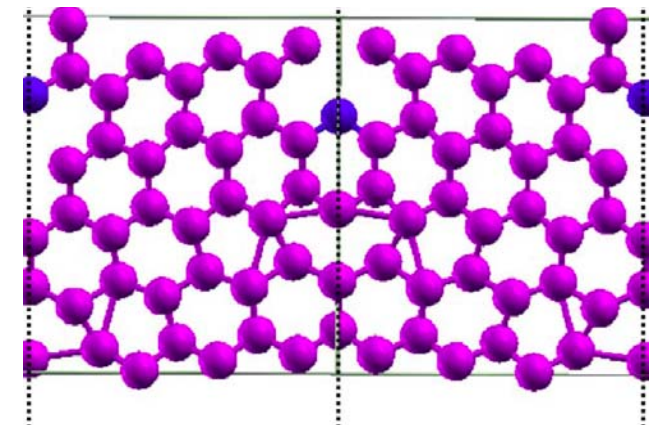
GB2: $(12\bar{3}0)[0001] \Sigma 7$



112 atoms

$$E_{GB2} = 1.89 \text{ J/m}^2$$

GB3: $(23\bar{5}0)[0001] \Sigma 19$

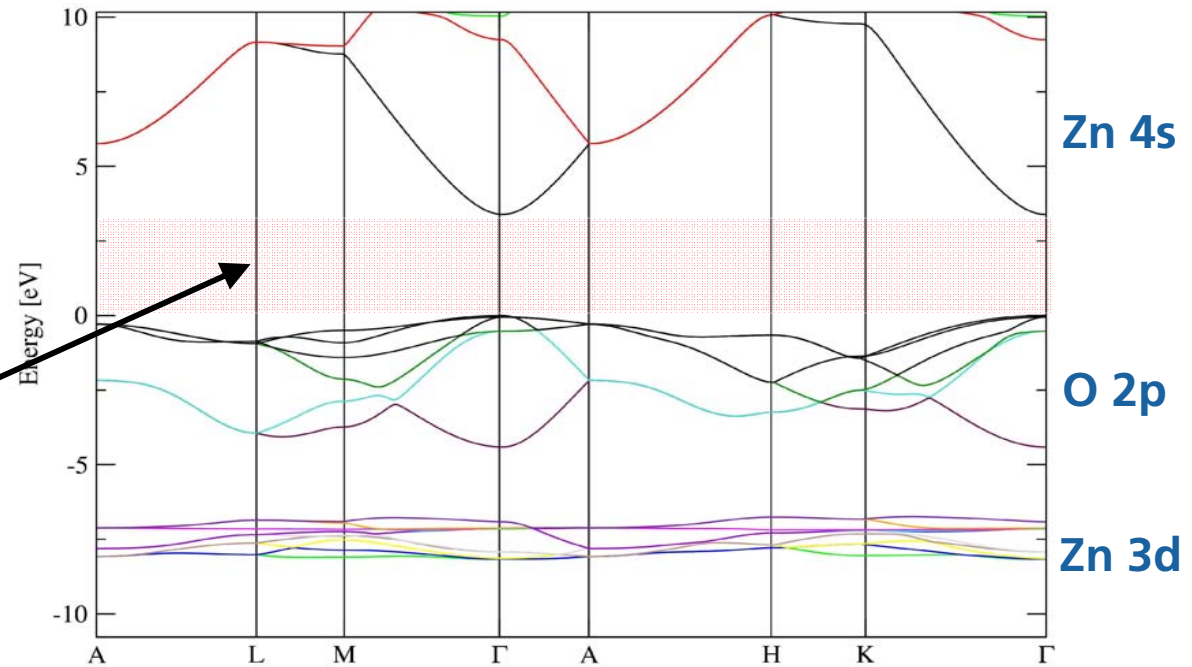


152 atoms

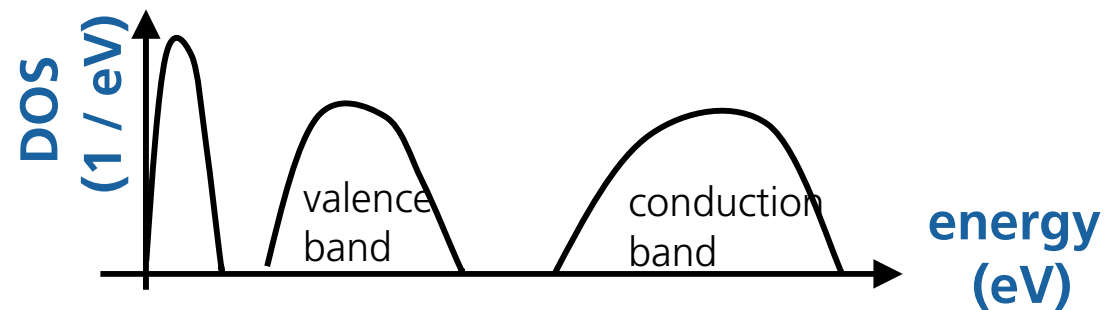
$$E_{GB3} = 1.65 \text{ J/m}^2$$

reference system: band structure of bulk ZnO

SIC-LDA

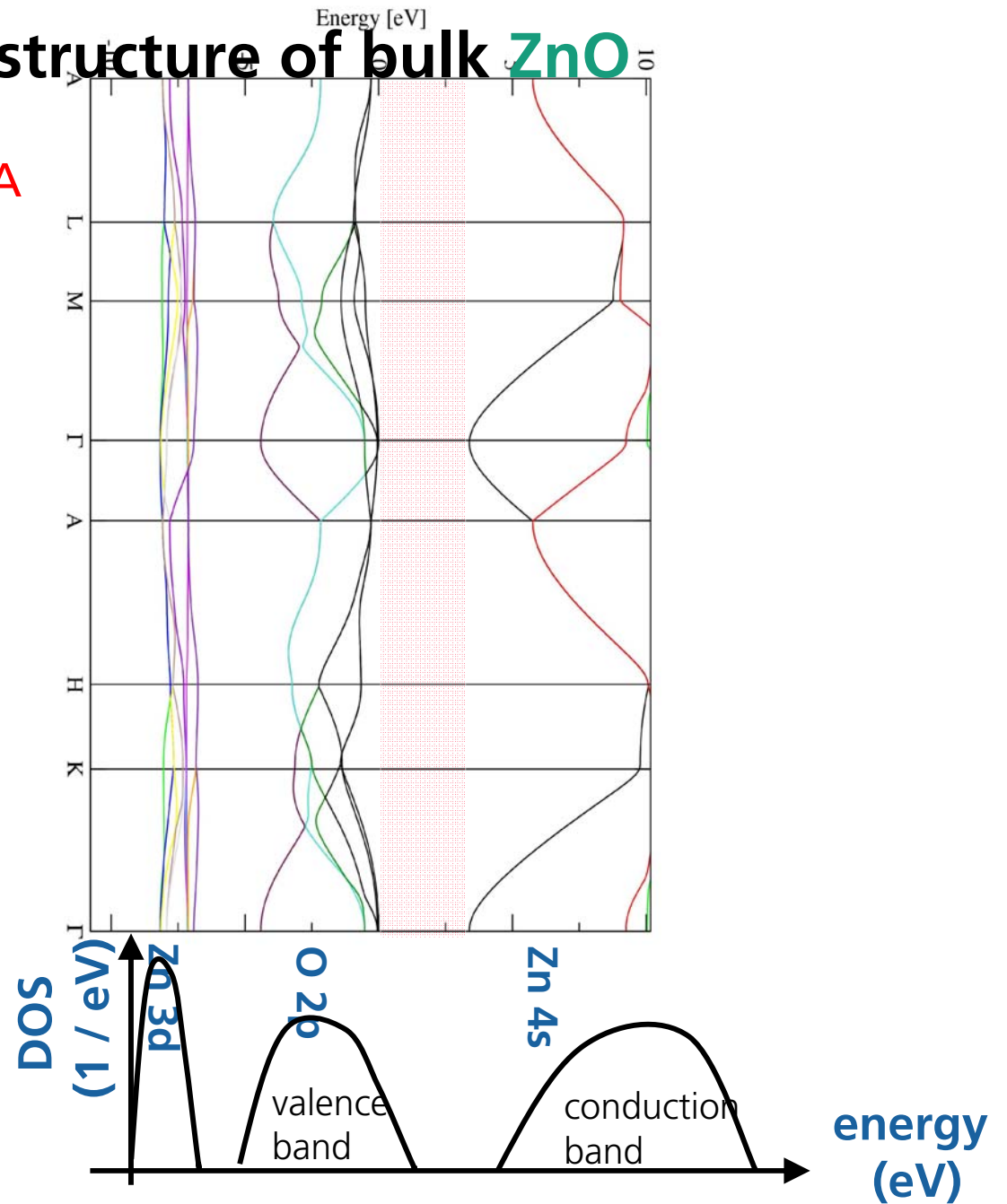


band gap 3.4 eV

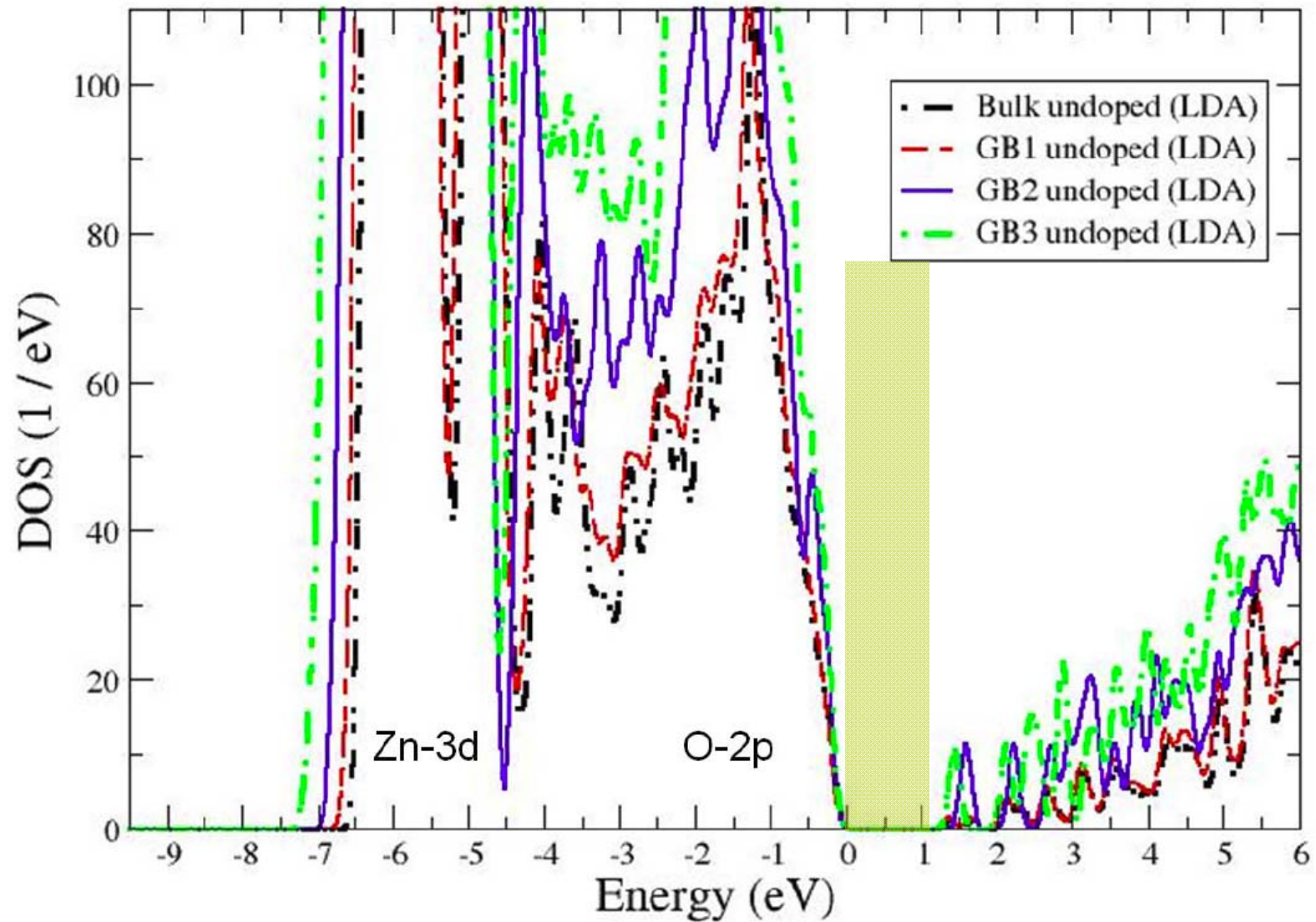


reference system: band structure of bulk ZnO

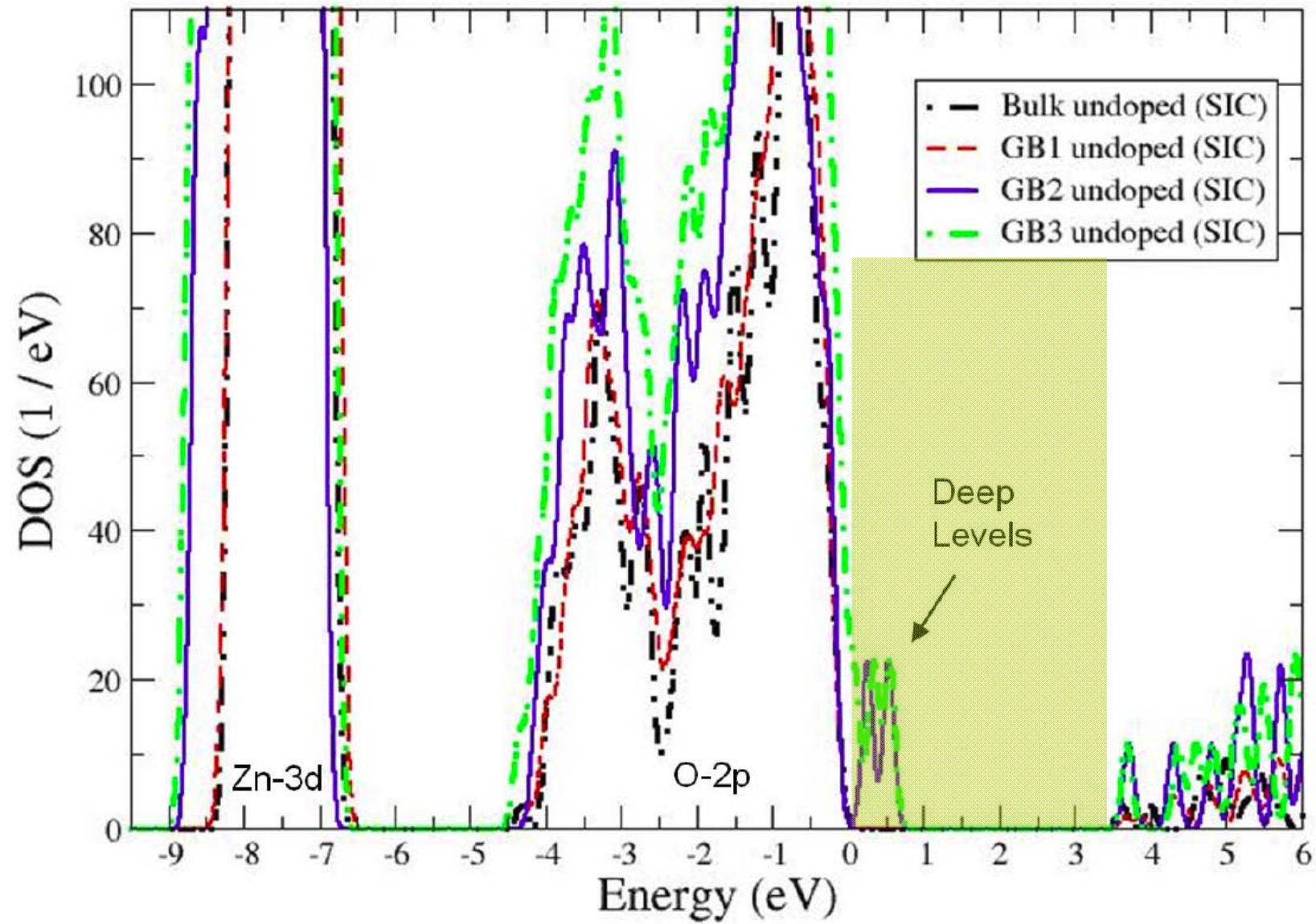
SIC-LDA



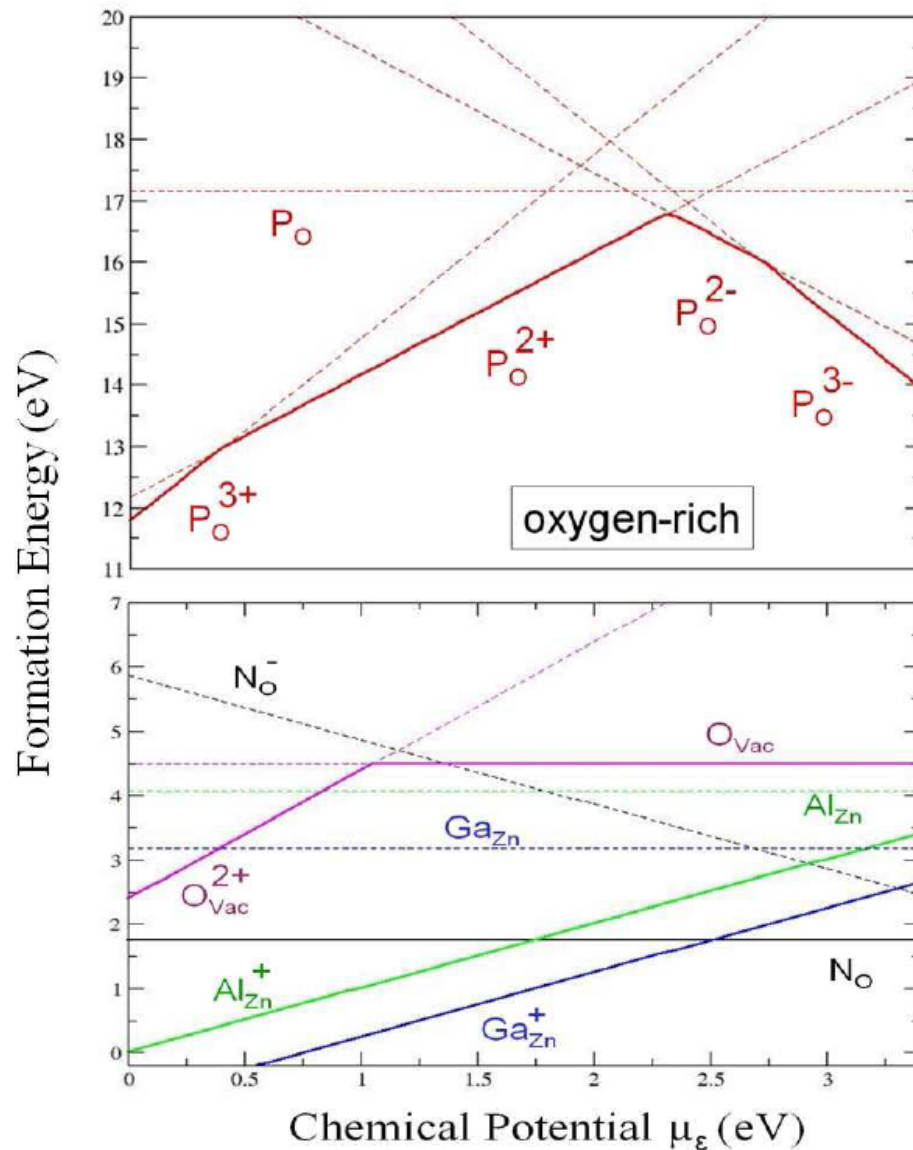
LDA: total DOS of undoped bulk and GB



SIC: total DOS of undoped bulk and GB



LDA + SIC: formation energies for dopants in bulk ZnO

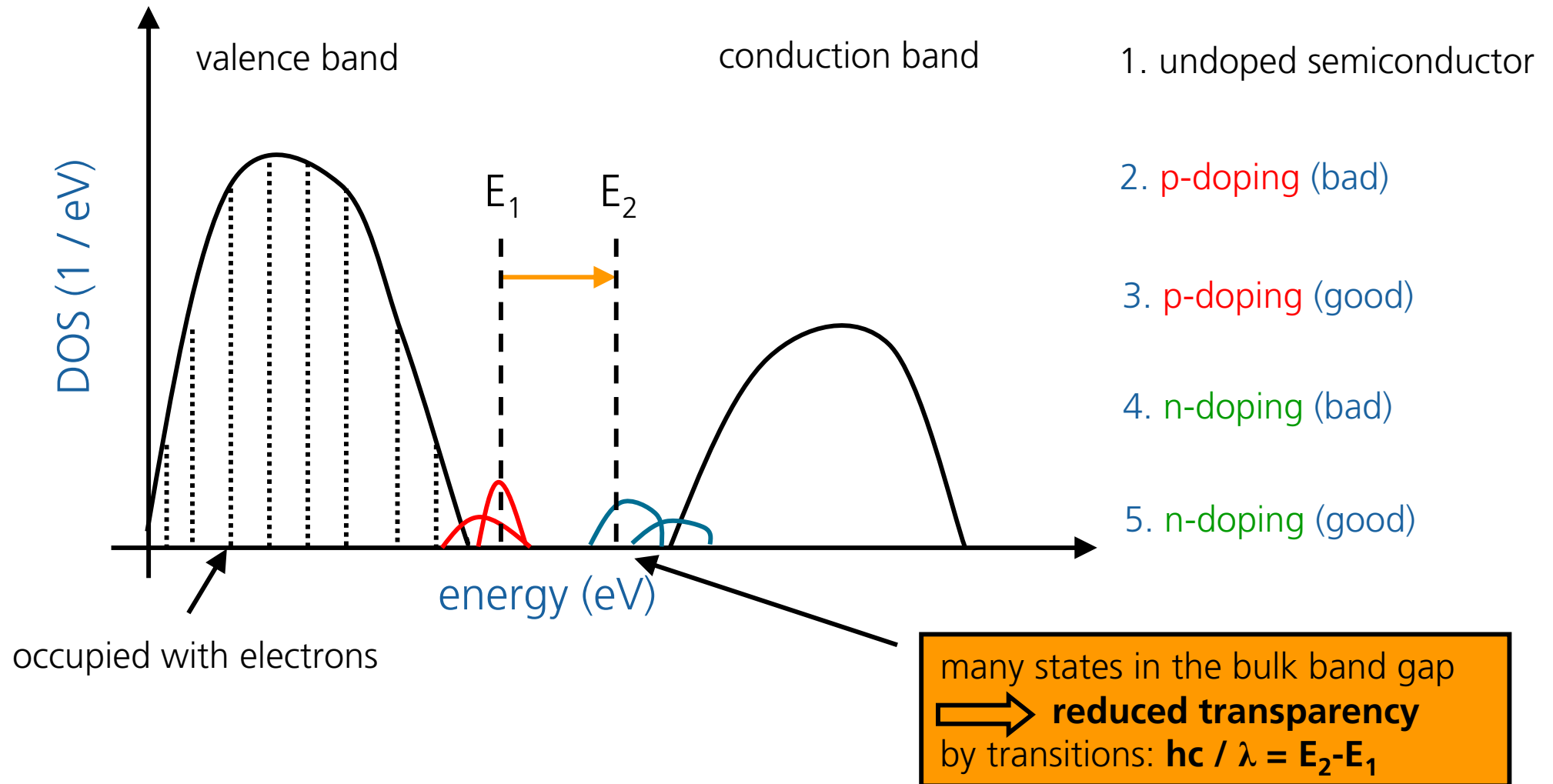


- For calculation of defect formation energies see, e.g.:
Van de Walle and Neugebauer
J. Appl. Phys. 95 (2003) 3851

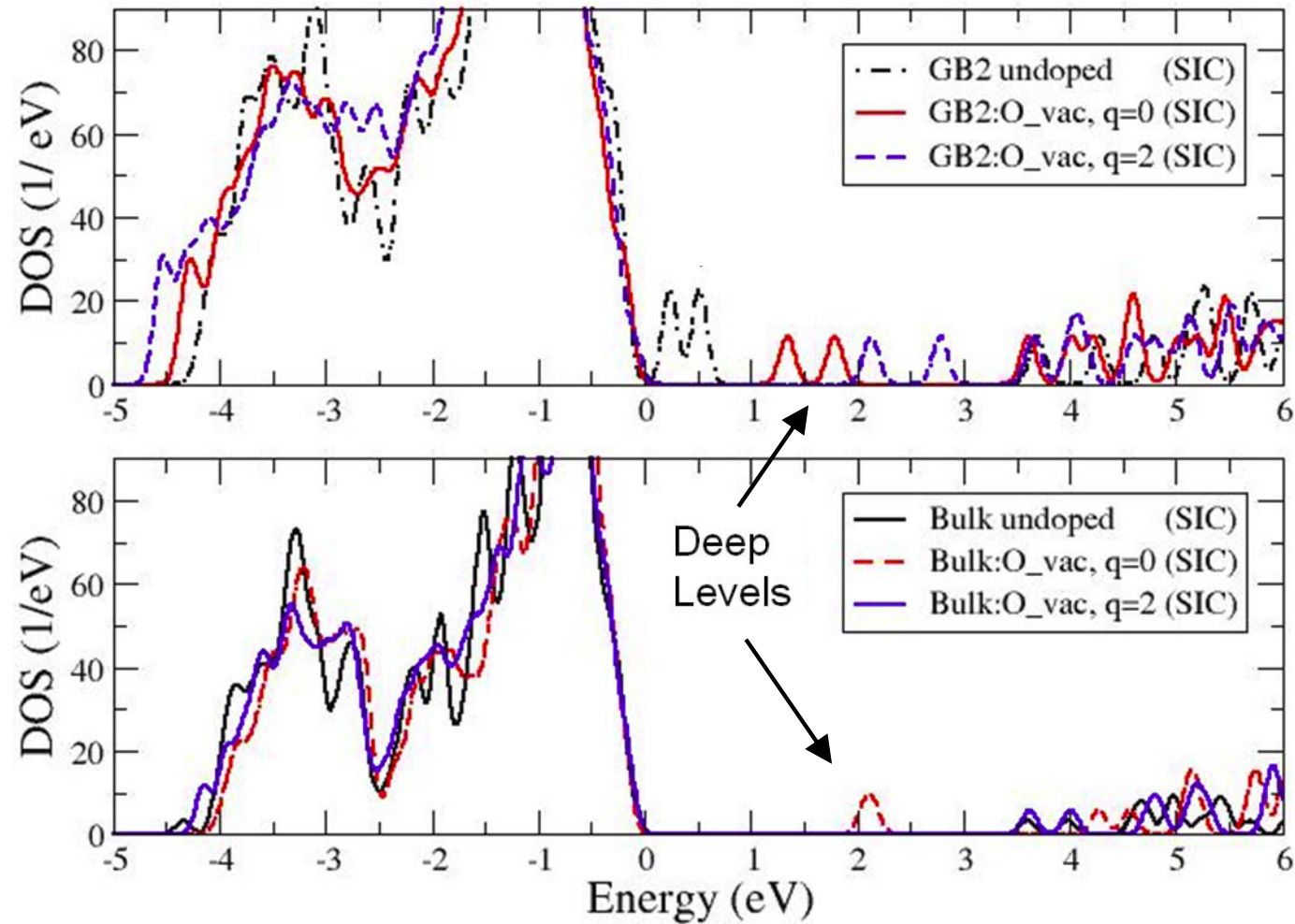
$$E_f^m(d, q) = E_{tot}^m(d, q) - E_{tot}^m(h, q = 0) + \mu(h) - \mu(d) - q\mu_e$$

- For discussions of O vacancy in bulk ZnO see, e.g.:
Lany and Zunger
Phys. Rev. B 78 (2008) 235104
Van de Walle
J. Phys.: Condens. Matter 20 (2008) 064230
- (Zn vacancy in bulk ZnO is "tricky" as well.)

indicators for conductivity and transparency in band structure



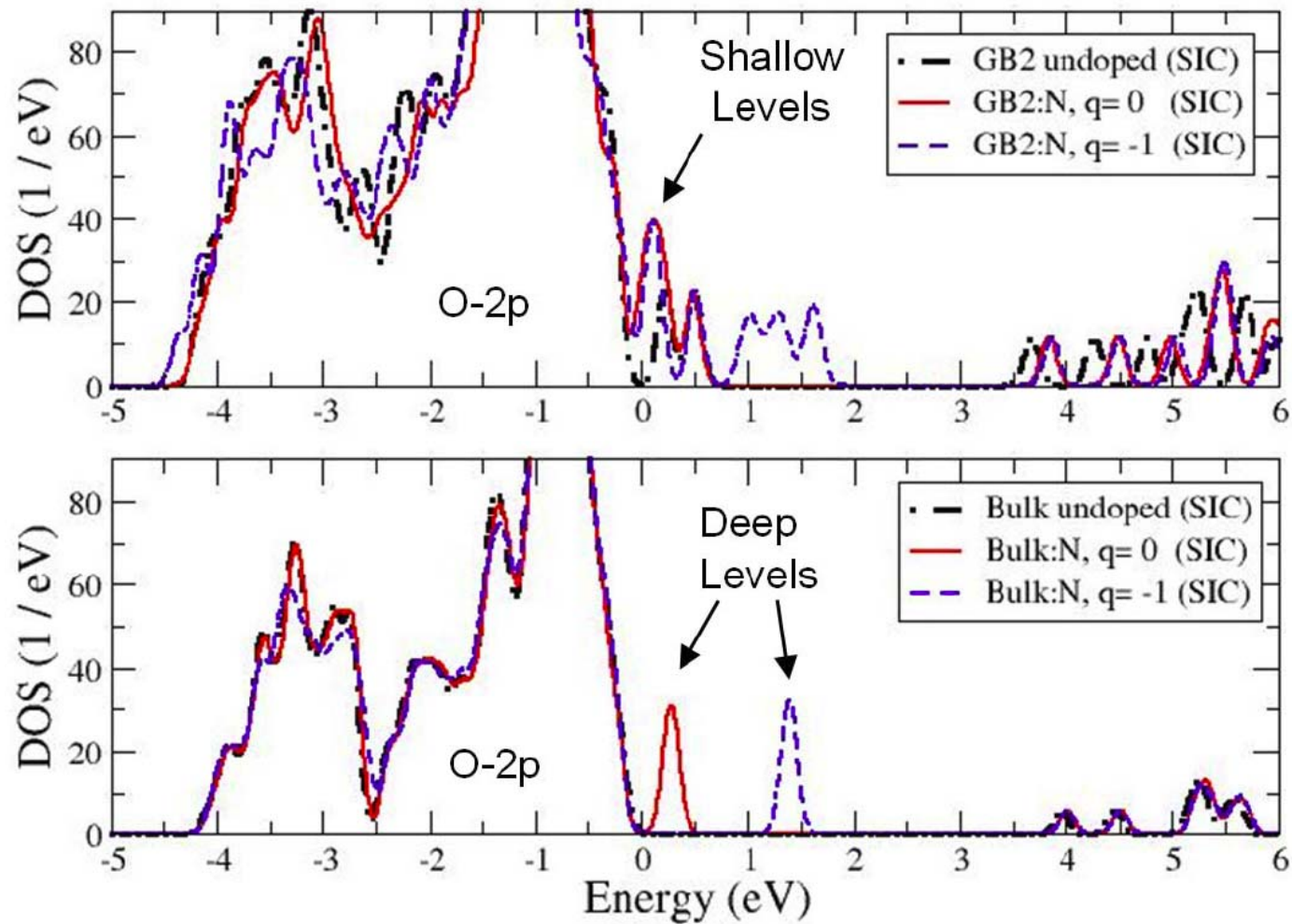
SIC: oxygen vacancy in ZnO



O_{vac} @ GB2:
bad conductivity,
and bad transparency

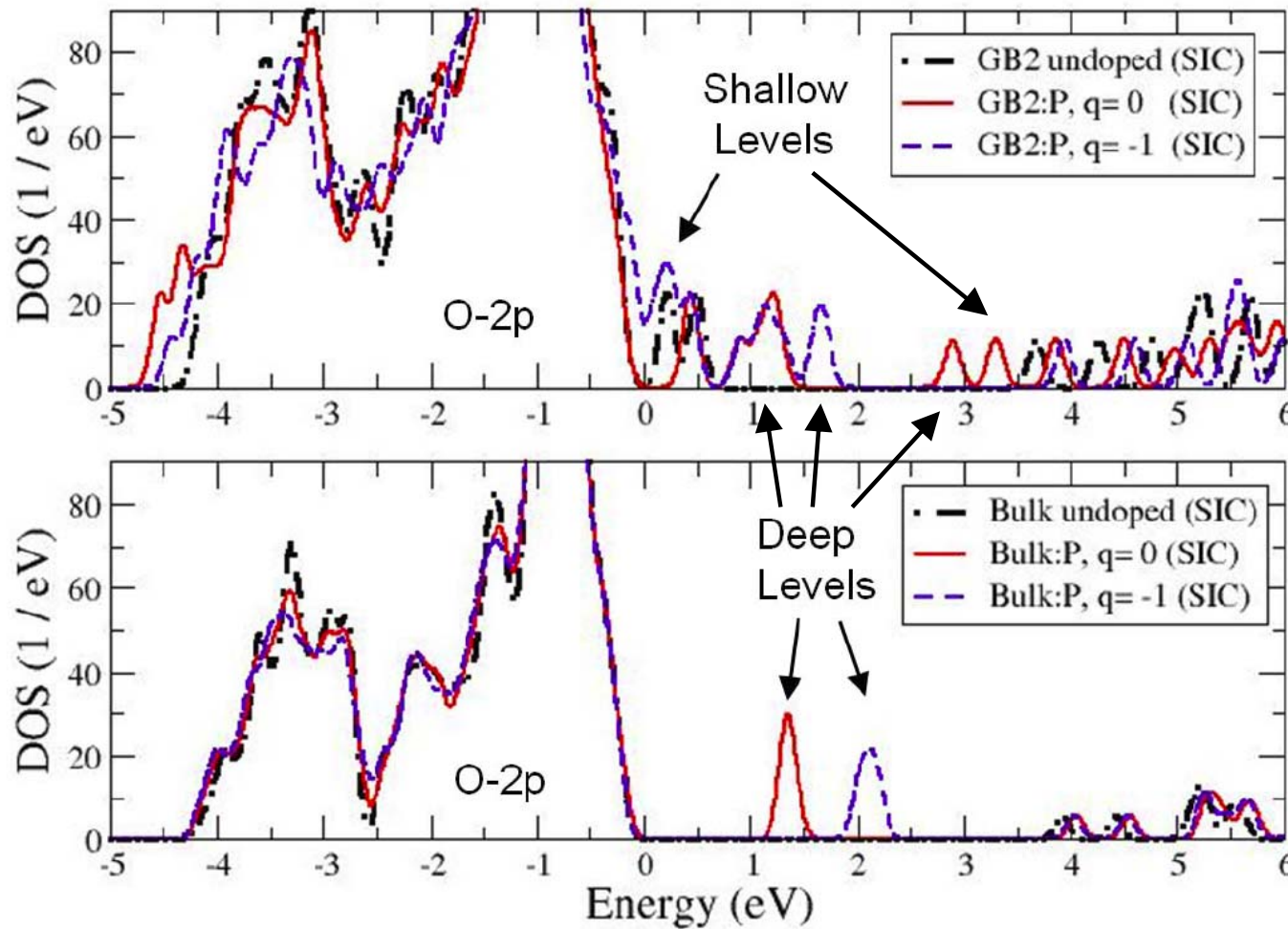
■ exp.: „green luminescence”
of ZnO with energy 2.4 eV

SIC: N_O dopant in ZnO



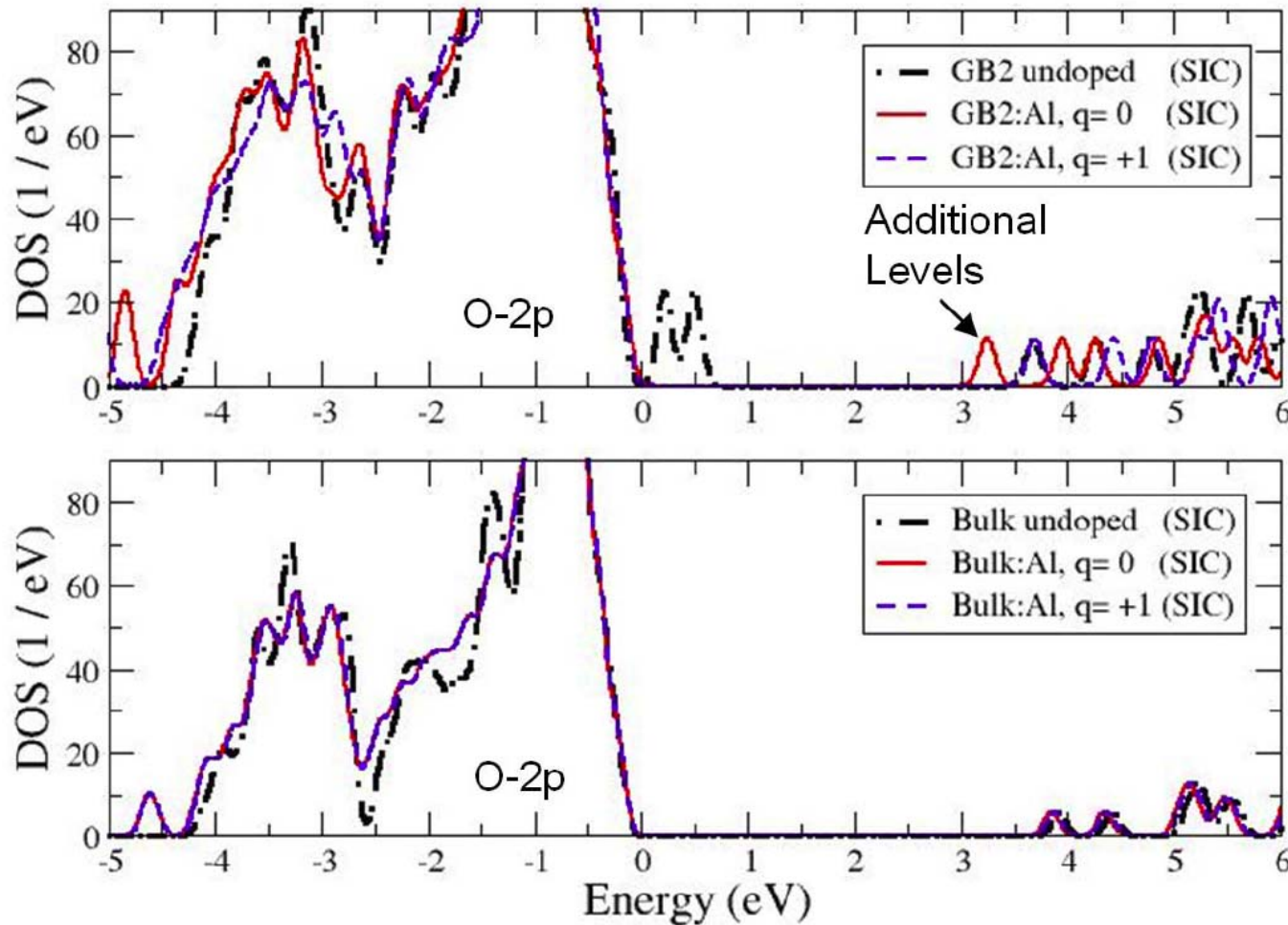
N_O @ GB2:
p-type conductivity at room temp. plausible, and good transparency

SIC: P_O dopant in ZnO



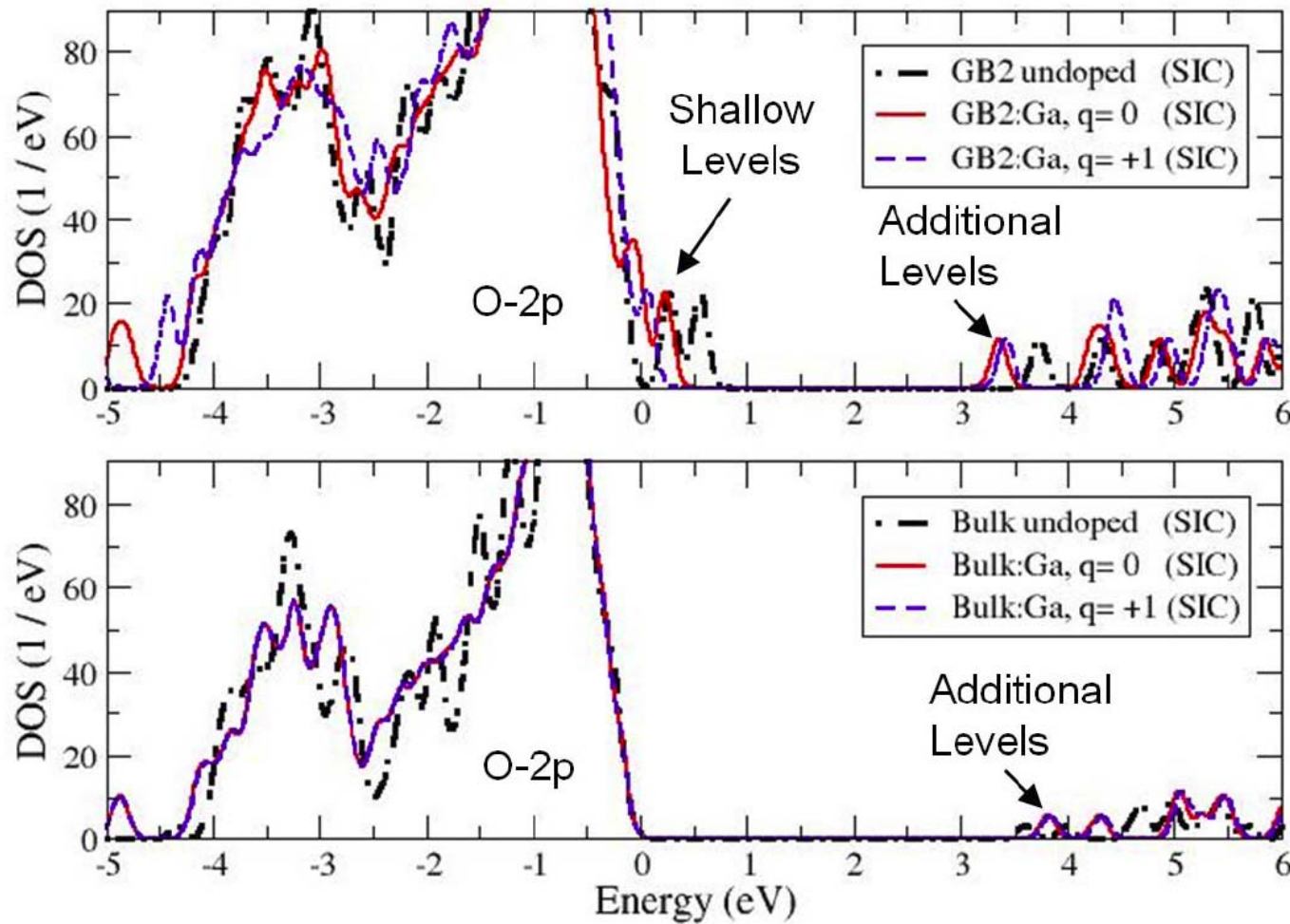
P_O @ GB2:
good conductivity,
but bad transparency

SIC: Al_{Zn} dopant in ZnO



Al_{Zn} @ GB2:
n-type conductivity at
room temp. plausible,
and good transparency

SIC: Ga_{zn} dopant in ZnO



Ga_{zn} @ GB2:
good conductivity,
and good transparency

Conclusion I: ZnO

- **SIC:** self interaction correction via pseudopotentials
 - can describe band structure of ZnO better than LDA.
 - It is applicable to extended structural defects like grain boundaries.
- **grain boundaries** in polycrystalline ZnO
 - can cause deep defect levels in the band gap.
 - This SIC result is different from others' and our LDA results for GB!
- **dopants at grain boundaries** in ZnO
 - can cause shallow defect levels in the band gap.
 - Considering grain boundaries, not only perfect crystals, may help for better understanding of dopants in TCO ceramics?

Reference: W. Körner, C. Elsässer, Phys. Rev. B 81 (2010) 085324

Funding: Fraunhofer Society

<http://www.transparente-elektroden.de/>

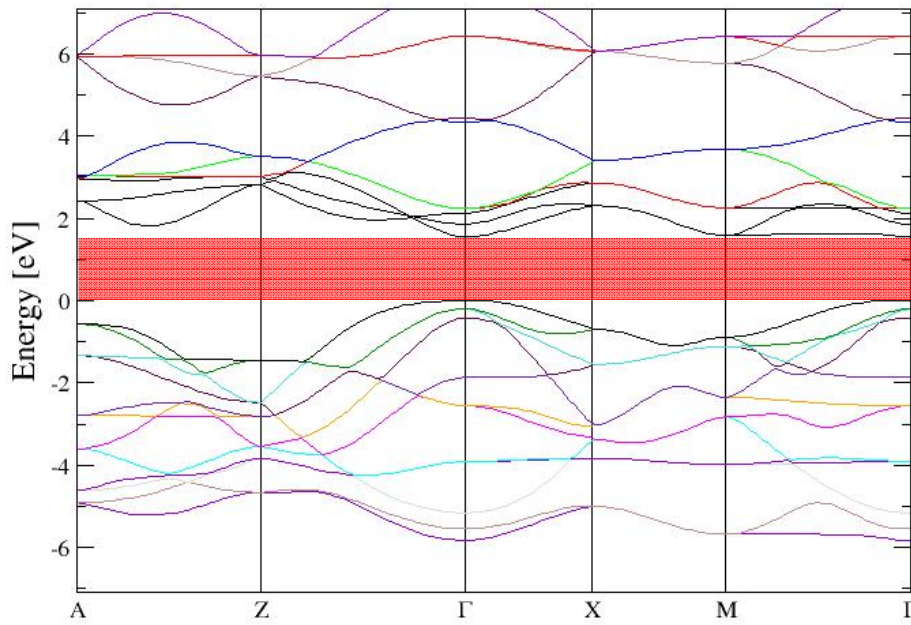
collection of supercell models for grain boundaries

material	boundary	interface	system size	γ [J/m ²]	
Wurtzite ZnO	(10 $\bar{1}0$)[10 $\bar{1}0$] Σ 1	[10 $\bar{1}0$] / 180°	80	0.17	GB1
	(12 $\bar{3}0$)[0001] Σ 7	[0001] / 21.79°	56 / 112	1.81/1.88	GB2
	(23 $\bar{5}0$)[0001] Σ 19	[0001] / 13.17°	152	1.65	GB3
Rutile TiO₂	(100)[100] Σ 1	[100] / 180°	72	0.47	GB1
	(210)[001] Σ 5	[001] / 36.87°	60 / 120	1.86/1.92	GB2
	(310)[001] Σ 5	[001] / 53.13°	120	2.37	GB3
Anatase TiO₂	(100)[100] Σ 1	[100] / 180°	72	0.64	GB1
	(021)[100] Σ 5	[100] / 78.46°	120	0.89	GB2
	(031)[100] Σ 5	[100] / 101.54°	120	2.36	GB3
	(120)[001] Σ 5	[001] / 53.13°	120	2.10	GB4

TiO₂: band structure of Rutile

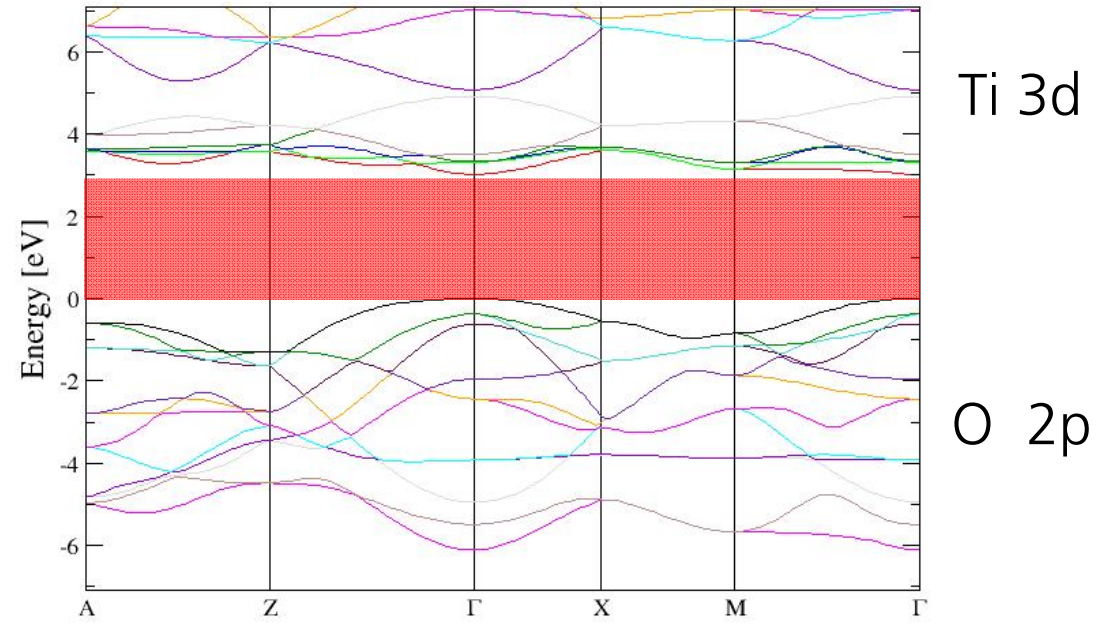
$E_{\text{gap}} = 3.04 \text{ eV (exp.)}$

LDA



$E_{\text{gap}} = 1.55 \text{ eV}$

SIC



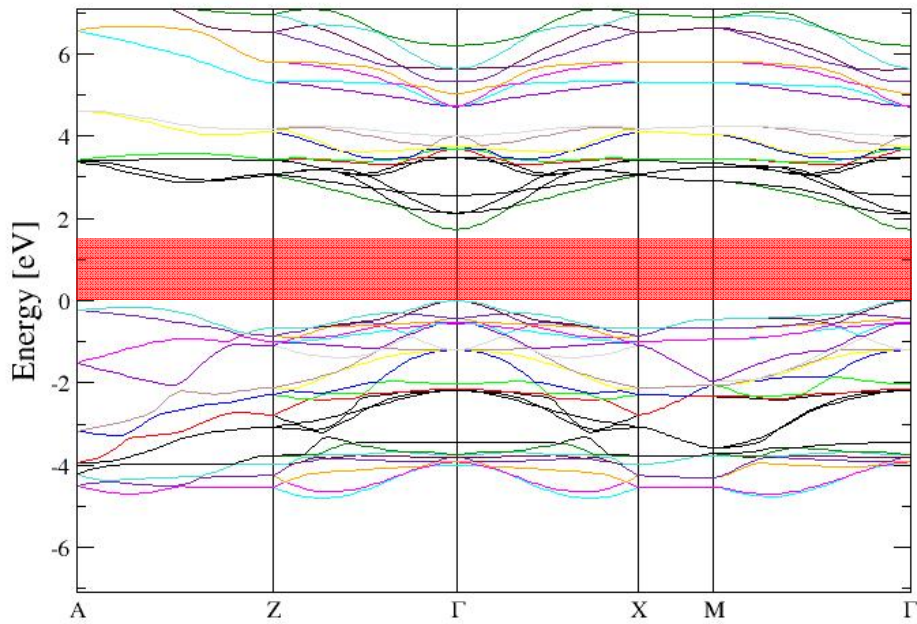
$E_{\text{gap}} = 3.02 \text{ eV}$

bulk SIC: **Ti** (LDA), **O-2s** 100%, **O-2p** 90%, $\alpha = 0.8$

TiO₂: band structure of Anatase

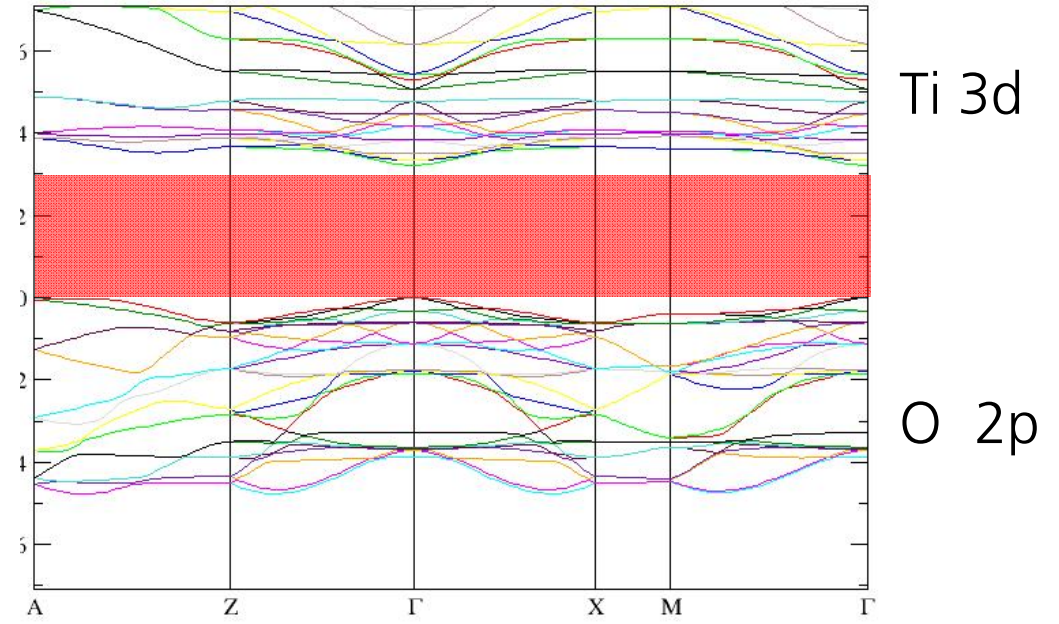
$$E_{\text{gap}} = 3.20 \text{ eV (exp.)}$$

LDA



$$E_{\text{gap}} = 1.73 \text{ eV}$$

SIC



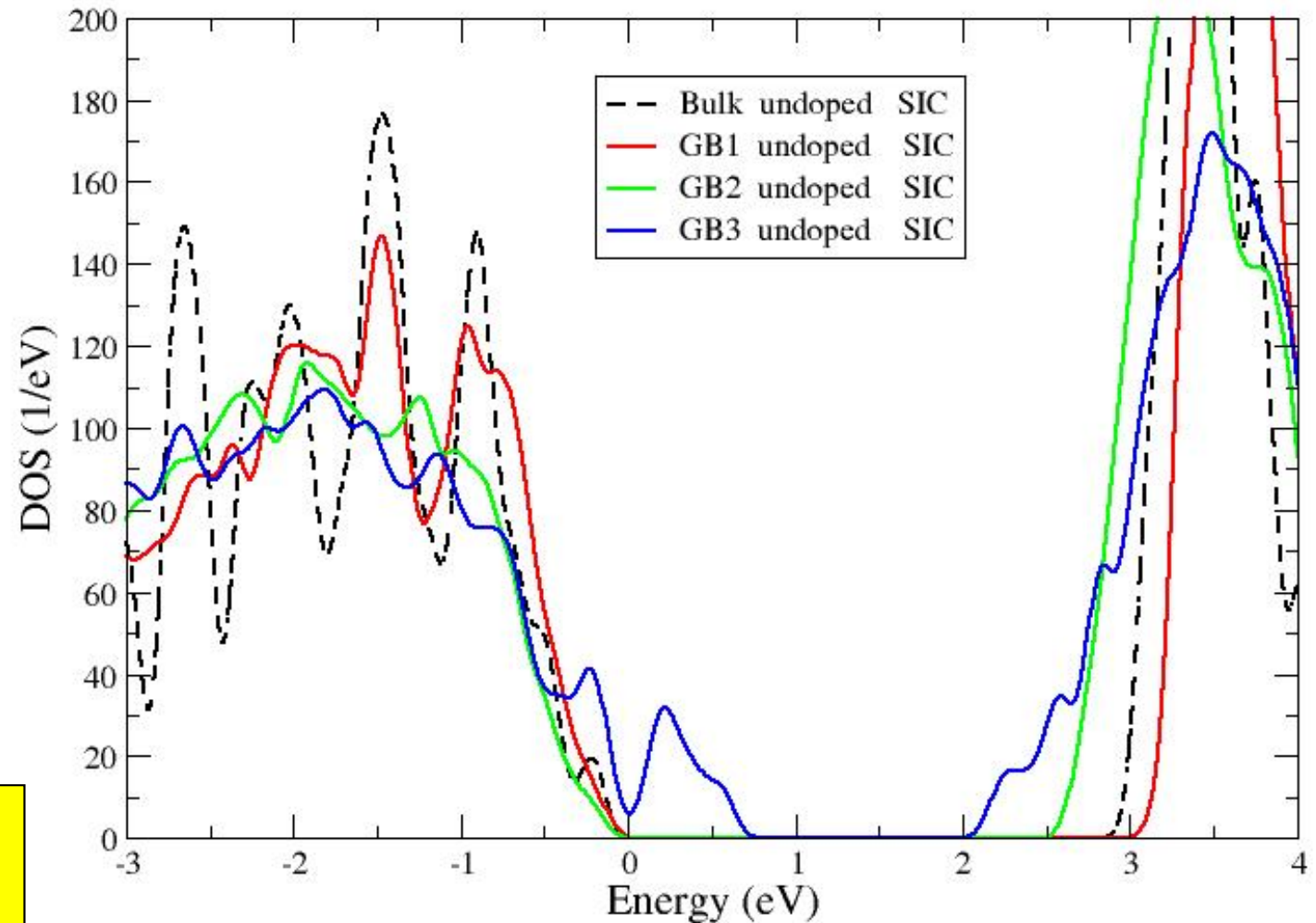
$$E_{\text{gap}} = 3.22 \text{ eV}$$

bulk SIC: **Ti** (LDA), **O-2s** 100%, **O-2p** 80%, $\alpha = 0.8$

DOS of undoped GB in TiO₂ (rutile)

SIC-LDA

- „deep levels“ for GB3
- GB1 is structually very similar to bulk

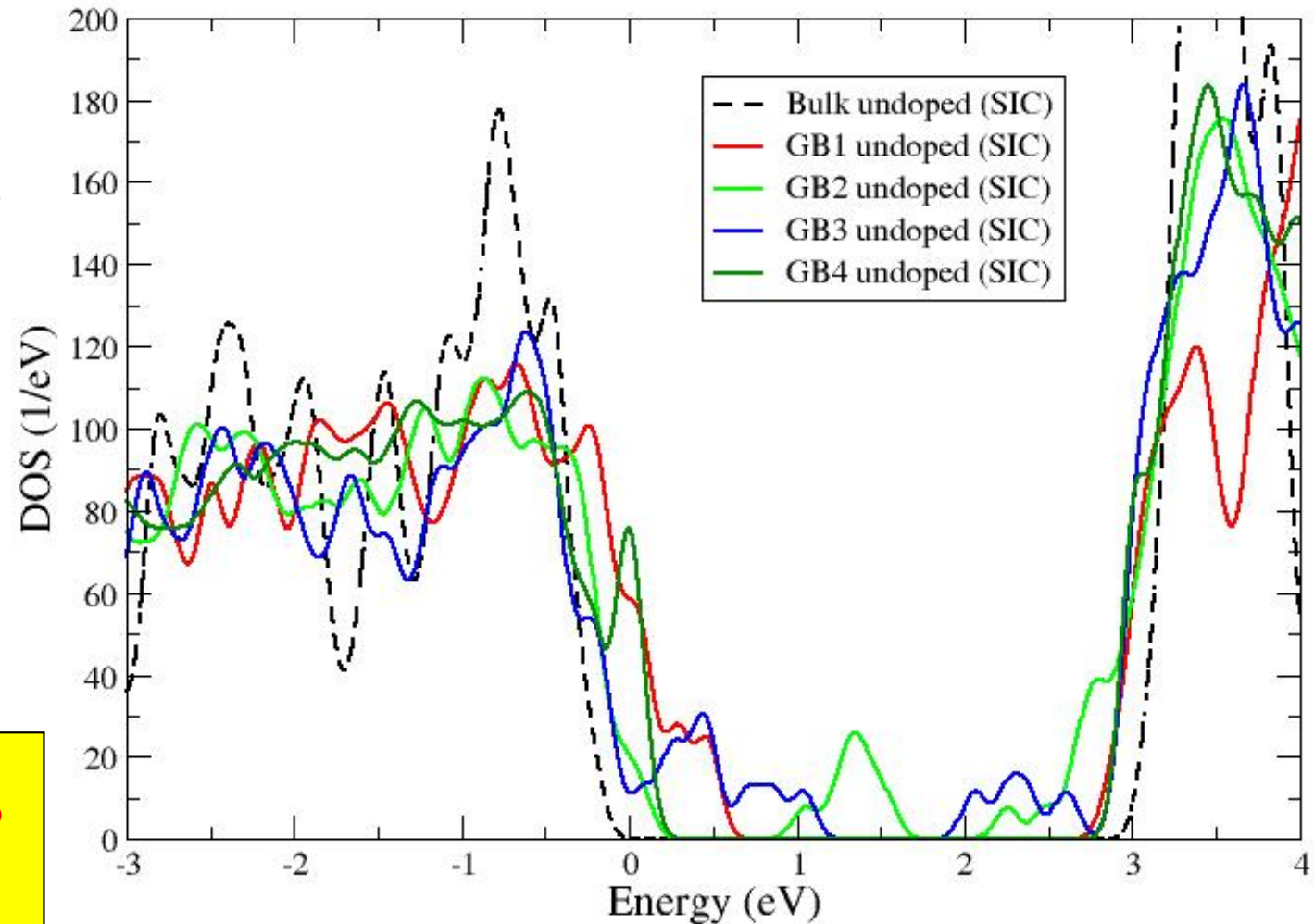


O atoms at GB3 have only **two** Ti atoms as nearest neighbours.

DOS of undoped GB in TiO_2 (anatase)

SIC-LDA

- „deep levels“
for GB1, GB2 and GB3

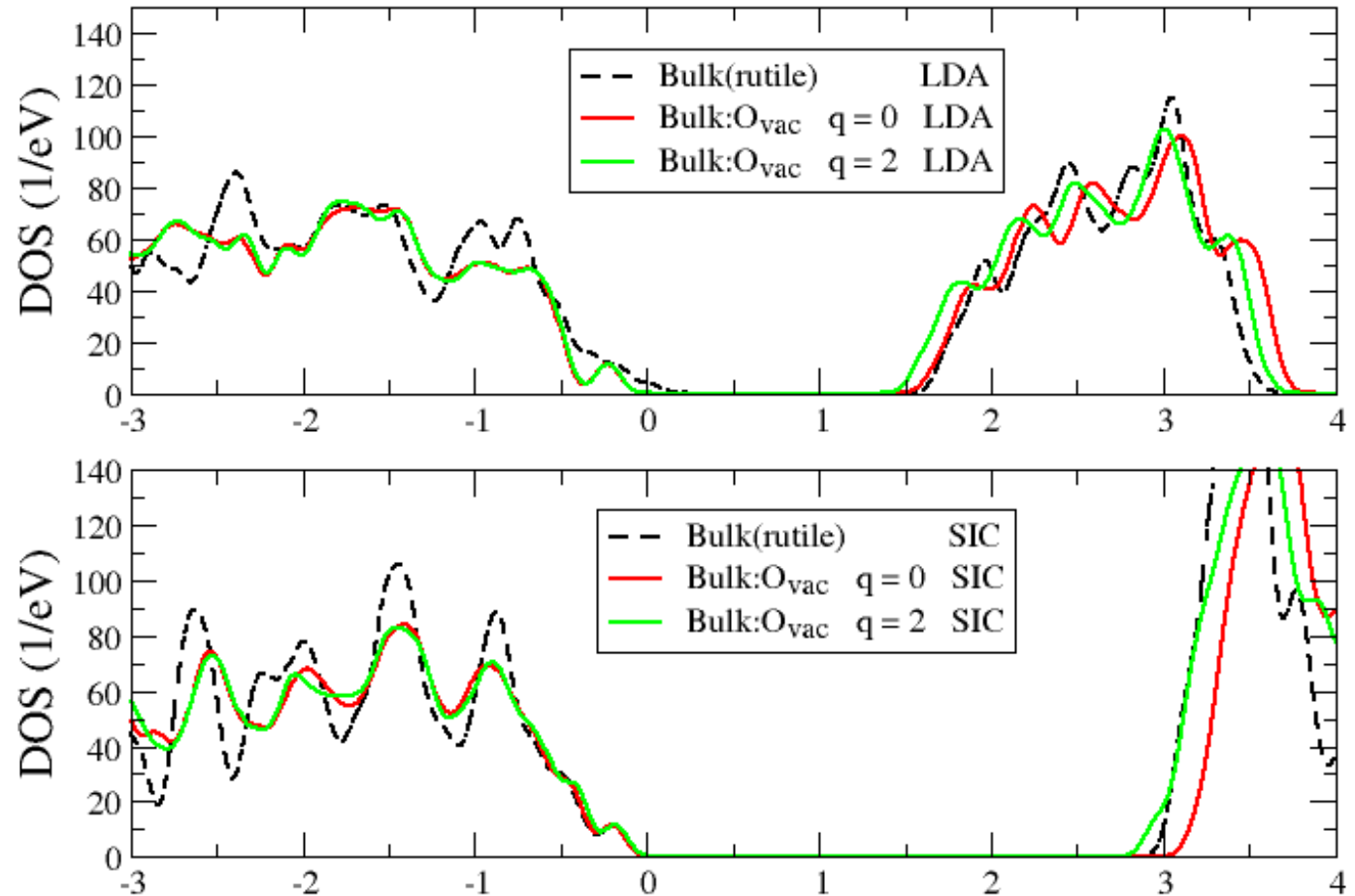


O atoms at GB1, GB2, and GB3 have only **two** Ti atoms as nearest neighbours.

O vacancy in TiO_2 (rutile)

comparison **LDA vs SIC**

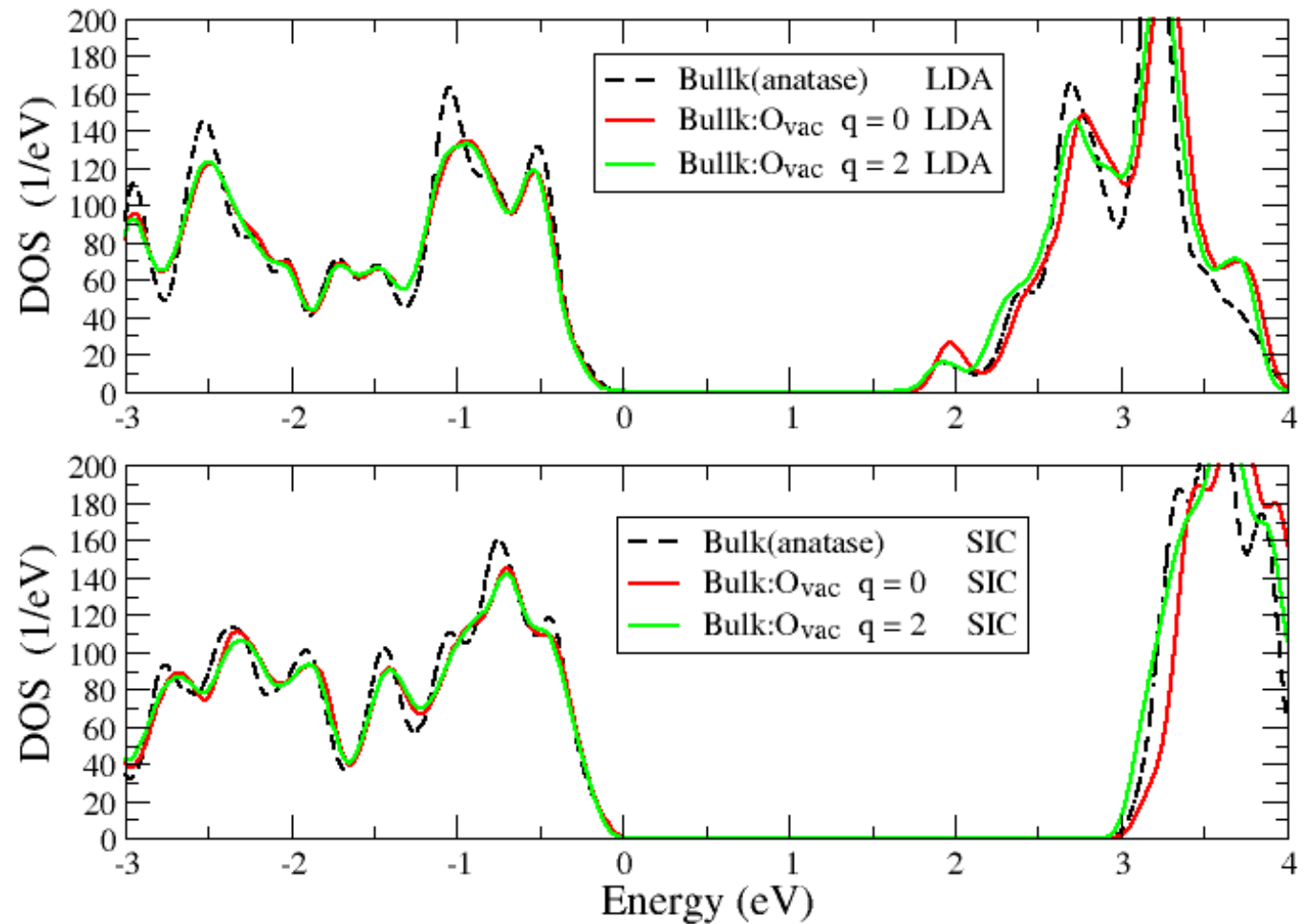
- no donor levels
(in accordance with other DFT studies)



O vacancy in TiO_2 (anatase)

comparison **LDA vs SIC**

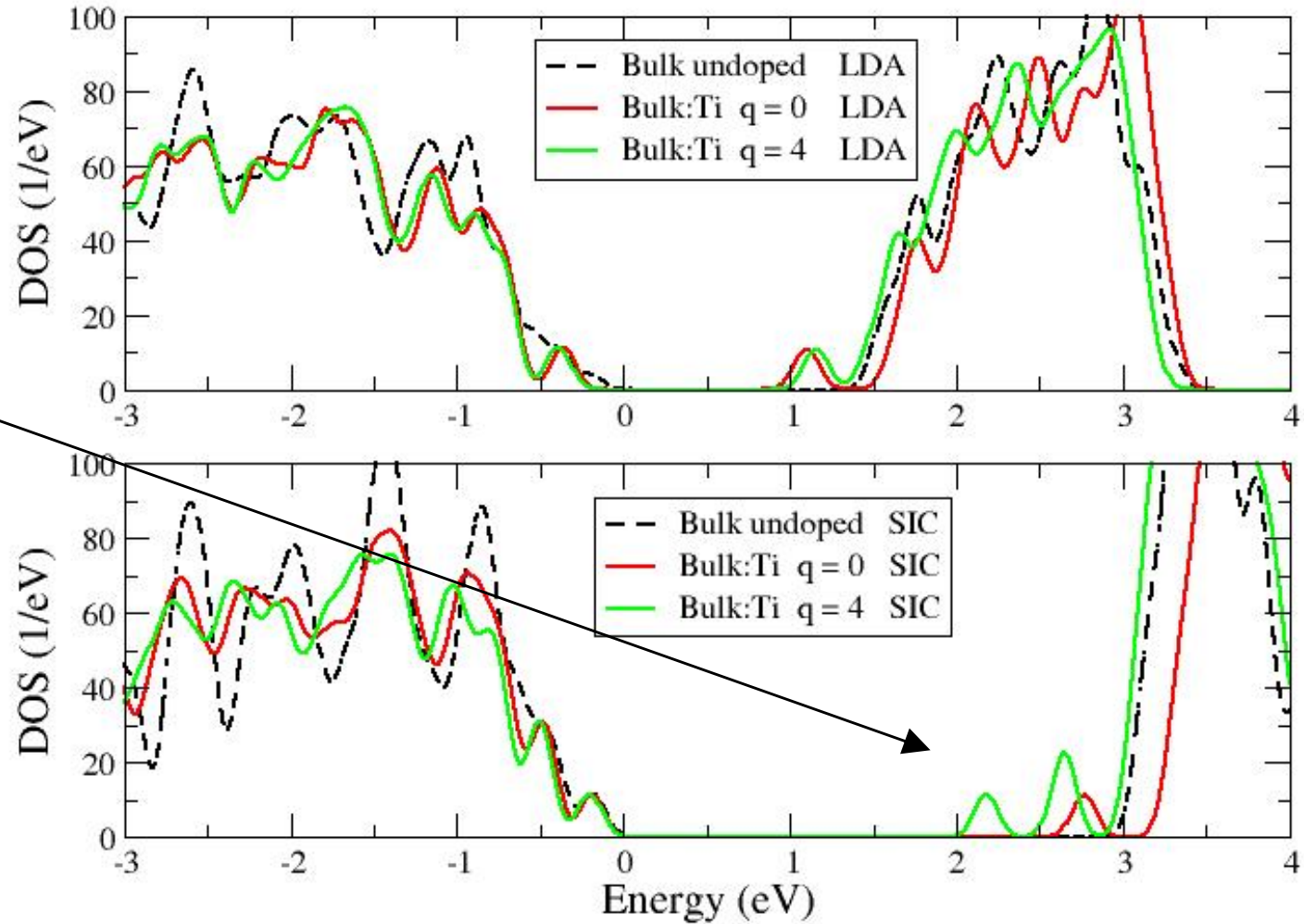
- no donor levels
(in accordance with other DFT studies)



Interstitial Ti atom in TiO₂ (rutile)

comparison LDA vs SIC

■ donor levels



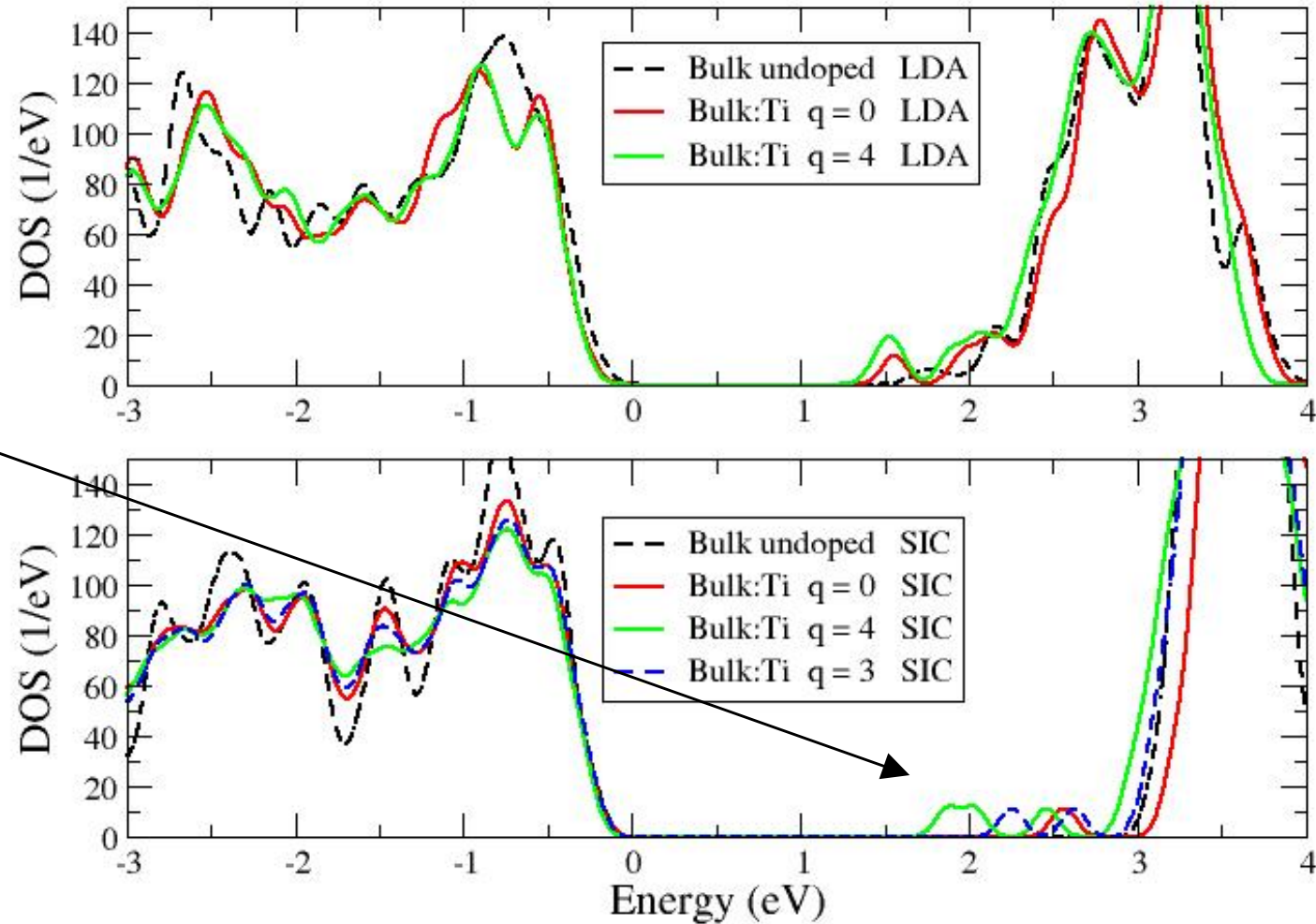
■ exp.: "blue coloration" of reduced TiO₂ (rutile) with energy 0.75eV

Cronemeyer et al. Phys. Rev. **82**, 975 (1951)

Interstitial Ti atom in TiO_2 (anatase)

comparison **LDA vs SIC**

■ donor levels



Hence:

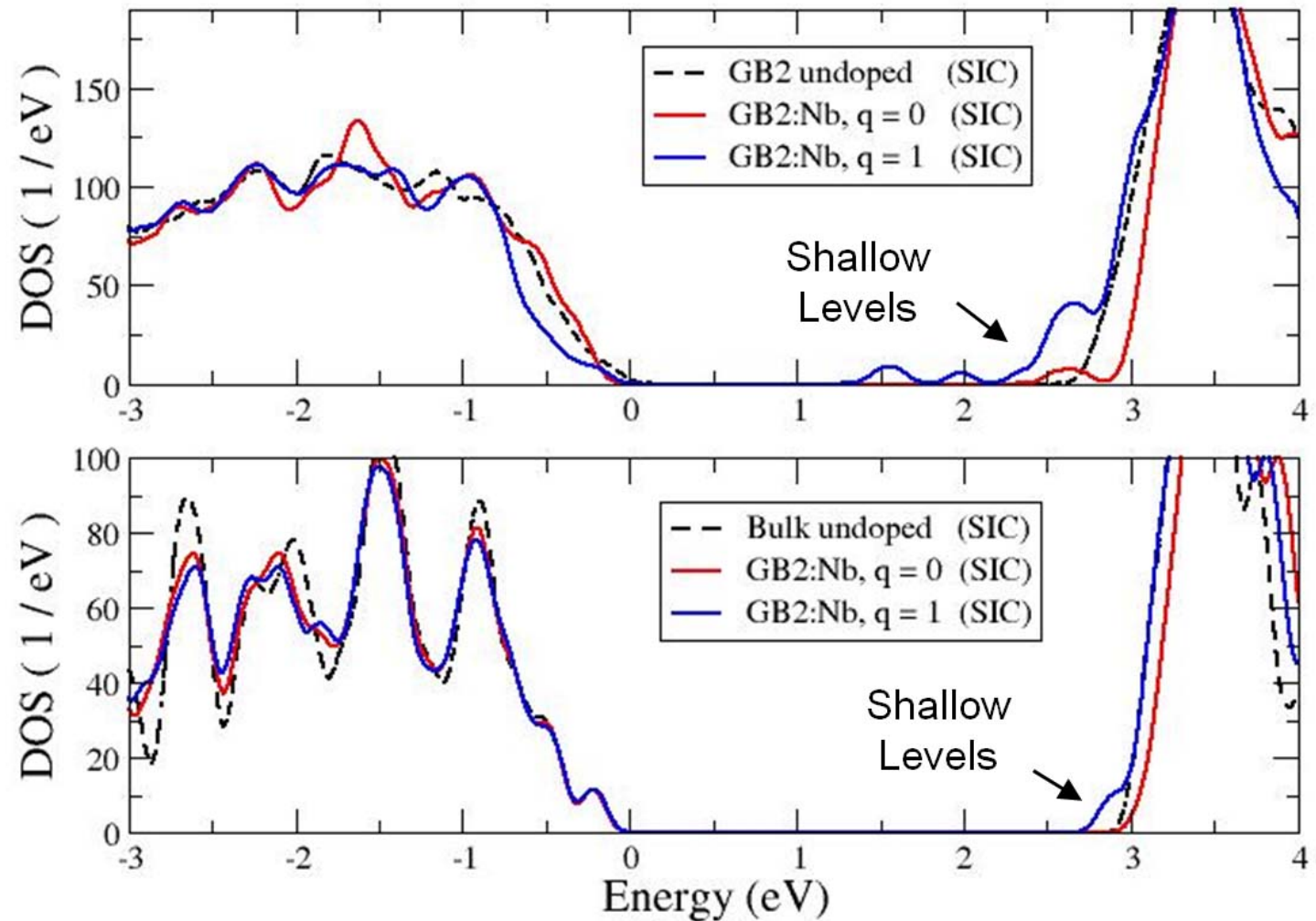
1. Anatase und Rutile show very similar behaviour.
2. Already LDA yields donor states.
3. SIC yields levels which could explain „blue coloration“.

TiO₂ (rutile) doped with Nb_{Ti}

comparison **bulk vs GB2**

■ Nb causes additional levels below the conduction-band edge.

➔ hence:
Nb is suitable for n-doping.

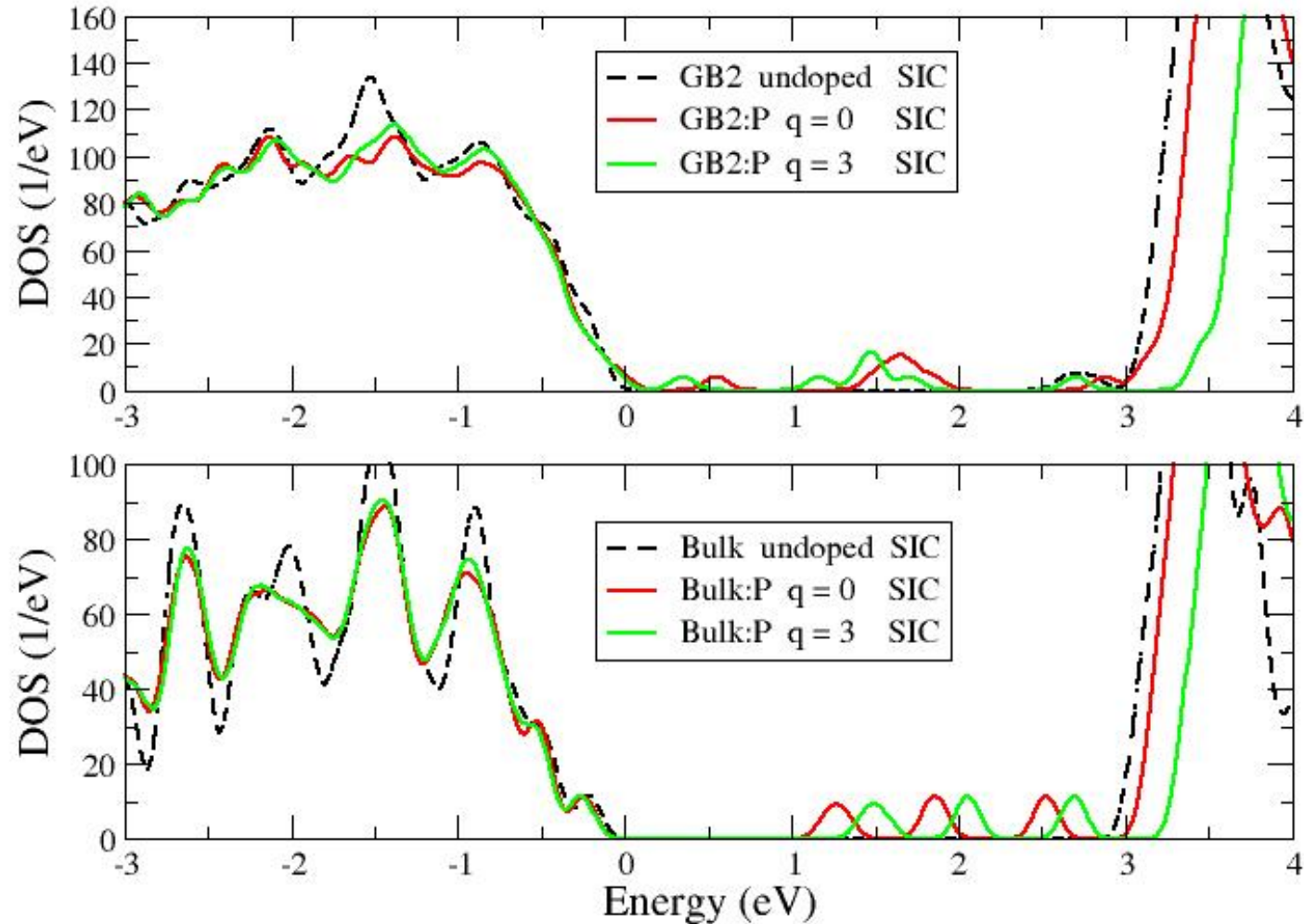


TiO₂ (rutile) doped with P_O

Vergleich Bulk vs GB2

■ At GB2 the additional levels are more smeared out than in bulk.

➔ nevertheless:
P is not suitable for p-doping.

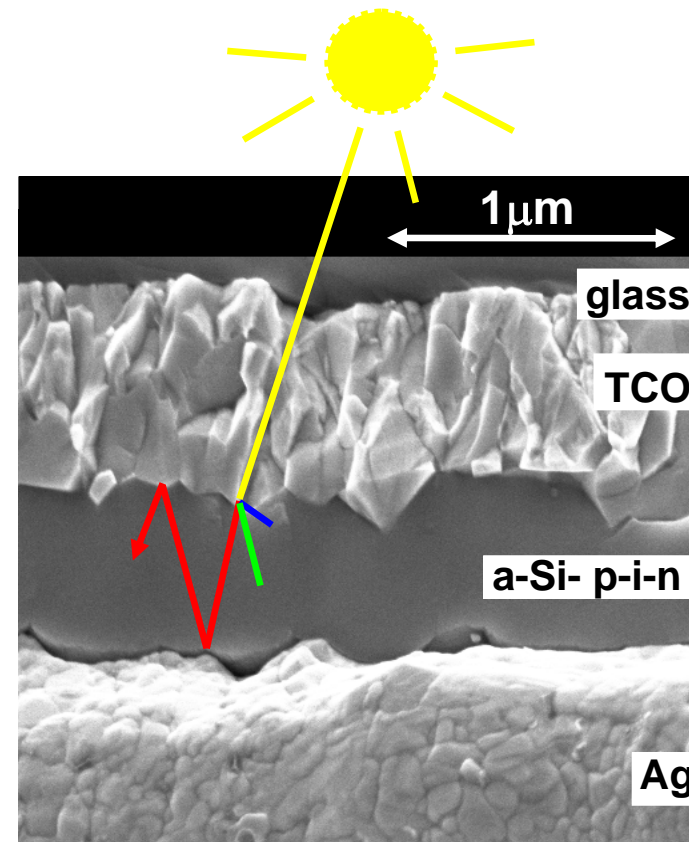
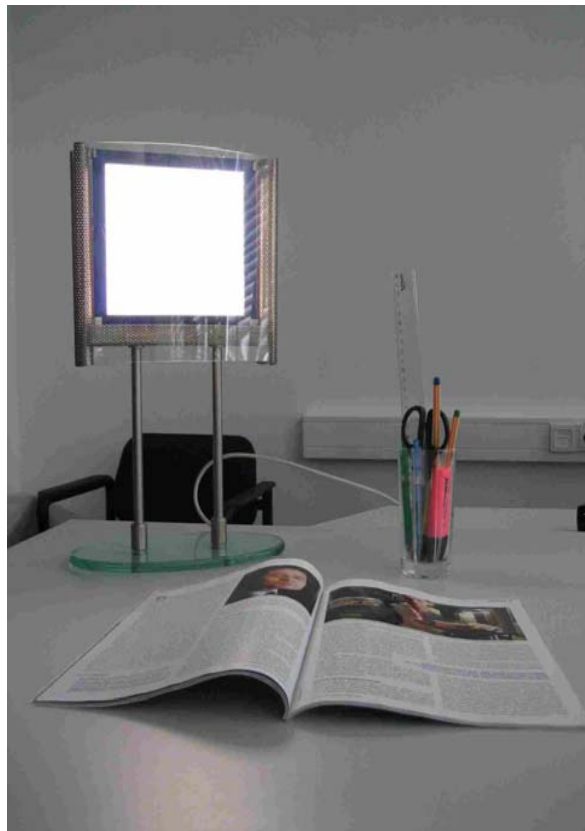


Conclusion II: ZnO and TiO₂

- Undoped grain boundaries of ZnO and TiO₂, which have O atoms with "dangling bonds", show "deep levels".
- TiO₂: Anatase and Rutile show only little differences.
- Intrinsic point defects
 - O-vacancy in ZnO and Ti-interstitials in TiO₂ may be related to n-conductivity.
 - experimental „green luminescence“ (2.4eV) of ZnO or "blue coloration" (0.75eV) of TiO₂ may be understood from theoretical SIC results.
- Extrinsic point defects
 - N is a good candidate for p-doping in both ZnO and TiO₂
 - Al and Ga are good candidates for n-doping in ZnO, Nb is the best found one in TiO₂.

First-principles DFT study of dopant elements at grain boundaries in the TCO materials ZnO and TiO₂

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Physical modelling of materials at Fraunhofer IWM



Matous
Mrovec



Adham
Hashibon



Jan Michael
Albina



Pavel
Marton



Wolfgang
Körner



Christian
Elsässer

$$\hat{H} \Psi = E \Psi$$



Tony
Paxton
(QUB)



Pierre
Hirel



Sabine
Körbel



Eva Marie
Kalivoda



Martin
Reese



Paul
Bristowe
(CAM)