Climate Dynamics Summer Semester 2017

UNIVERSITÄT LEIPZIG

Homework 3 Due 10 May 2017

Problem 1 Saturation water vapor pressure

Consider the Clausius-Clapeyron equation, (2.65):

$$\frac{d\ln e_s}{dT} = \frac{L}{R_v T^2} \tag{1}$$

- (a) Show that e_s increases by approximately 7% K⁻¹ for typical values of the near-surface air temperature.
- (b) Approximately how large of a temperature increase is required for es to double?

Problem 2 Diabatic heating

Starting with the thermodynamic energy equation (2.46),

$$c_{p}\frac{dT}{dt} = T\frac{ds}{dt} + \alpha \frac{dp}{dt} = Q + \alpha \omega, \qquad (2)$$

show that an equivalent formulation (involving the static stability $\partial \theta / \partial p$) is

$$c_{pd}\frac{T}{\theta}\left(\frac{\partial\theta}{\partial t} + \vec{\mathbf{v}}\cdot\nabla_{p}\theta + \omega\frac{\partial\theta}{\partial p}\right) = Q$$
(3)

Problem 3 Averaging operators

The temporal mean of an arbitrary field A over a time period au is defined as

$$\overline{A} = \overline{A}(\lambda, \phi, p) = \frac{1}{\tau} \int_{-\tau/2}^{\tau/2} A(\lambda, \phi, p, t) dt$$
(4)

The zonal mean (over all longitudes) is defined as

$$[A] = [A](\phi, p, t) = \frac{1}{2\pi} \int_0^{2\pi} A(\lambda, \phi, p, t) \, d\lambda$$
(5)

The instantaneous value of A is given by

$$A = \overline{A} + A' \tag{6}$$

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where A' is called the *fluctuating* component of A. Likewise

$$A = [A] + A^* \tag{7}$$

where A* is the departure from the zonal mean. Show that for arbitrary fields A and B

(a) $A = \left[\overline{A}\right] + \left[A'\right] + \overline{A}^* + A'^*$ (b) $\left[\overline{AB}\right] = \left[\overline{A}\right] \left[\overline{B}\right] + \left[\overline{A}^*\overline{B}^*\right] + \left[\overline{A'B'}\right]$

Problem 4 Thermodynamic structure of the atmosphere

ERA Interim reanalysis air temperature data is available in the file

/home_local/quaas/data/ERA__Interim_T_GDS0_ISBL_123__1.5x1.5xL37__198901-200712.nc. Calculate zonal and temporal means of the following quantities and plot them as contour lines in the ϕ -p plane:

- (a) T
- (b) θ
- (c) q_s ; you may use the empirical approximation

$$e_{s}(T) = 6.1094 \exp\left(\frac{17.625T}{T + 243.04}\right)$$
(8)

for T in Celsius.

(d) θ_e