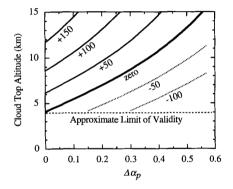
### Clouds



#### Clouds have two effects:

- pprox -50 W m $^{-2}$  Increased reflection of shortwave ( $\Delta lpha$ ) ightarrow cooling
- $\approx +20~\text{W m}^{-2}~\text{Colder longwave emission temperature} \rightarrow \text{warming}$

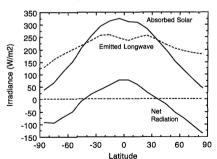
so that the sign of the cloud contribution to the radiative balance depends on cloud top temperature and cloud thickness

- SCu Thick, low clouds (like stratocumulus) have a large cooling effect
  - Ci Thin, high clouds (like cirrus) have a large warming effect

#### Zonal-mean radiative balance at TOA

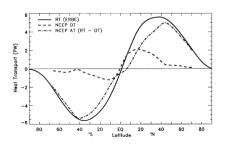
#### TOA radiative balance...

- The top-of-atmosphere (TOA) radiative balance measures how much energy enters or leaves the climate system
- In the tropics, the net energy flux is positive (into the climate system)
- In the extratropics, the net energy flux is negative (out of the climate system)

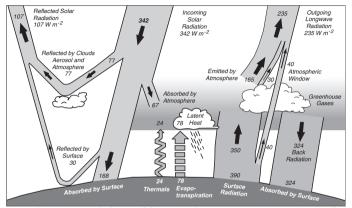


# ... requires meridional energy transport

- To maintain a steady state (e.g., constant long-term zonal-mean temperature), energy transport from the tropics into the extratropics is required
- ► The meridional divergence of the energy transport balances the radiative energy flux
- Contributions to transport from ocean and atmosphere subject of the next section



# Energy fluxes into and out of the atmosphere



Radiative energy balance of the atmosphere (sign convention: downwelling positive) is

$$R_a = F_{TOA} - F_s + R_{TOA} - R_s = (342 - 107) - 168 + (-235) - (324 - 390) \text{ W m}^{-2}$$
  
=  $\mathcal{O}(-100 \text{ W m}^{-2})$ , (5.12)

balanced by fluxes of sensible and latent heat into the atmosphere

# Today's Lecture: General circulation of the atmosphere

#### Reference

Hartmann, Global Physical Climatology (1994), Ch. 2, 3, 6 Peixoto and Oort, Ch. 4, 6, 7, 14, 15

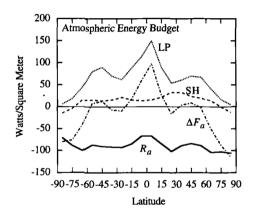
# 5.2 – General circulation of the atmosphere

- ► Atmospheric transport in response to radiative imbalance
- ► Mean meridional circulation and eddy circulation
- Energy cycle
- Entropy cycle

### 5.2 – General circulation of the atmosphere

- ► Atmospheric transport in response to radiative imbalance
- ► Mean meridional circulation and eddy circulation
- Energy cycle
- Entropy cycle
- ► Cycles of momentum, angular momentum
- Hydrological cycle

## Radiative balance requires atmospheric transport



- As we saw in the previous section, the net radiative energy balance of the atmosphere is  $R_a = \mathcal{O}(-100 \text{ W m}^{-2})$ ; the balance is fairly constant in latitude
- The radiative energy loss is balanced by latent (LP) and sensible (SH) heat flux from land and ocean; but these are strong functions of latitude
- Meridional advective atmospheric energy flux is required to provide local energy balance:

$$\Delta F_a + R_a + F_{LH} + F_{SH} = 0 \tag{5.13}$$

The advective energy flux is the meridional divergence of the meridional heat transport (sign convention: northward positive):

$$\frac{dN}{d\phi} = \int_0^{2\pi} d\lambda \, R_E^2 \, \Delta F_{\sigma}(\phi) \cos \phi = 2\pi R_E^2 \, \Delta F_{\sigma}(\phi) \cos \phi$$
(5.14)

#### Streamfunction

The zonal-mean continuity equation (zonal flow is integrated out) is

$$\frac{1}{R_{E}\cos\phi}\frac{\partial}{\partial\phi}([\bar{\mathbf{v}}]\cos\phi) + \frac{\partial[\bar{\omega}]}{\partial\rho} = 0$$
 (5.15)

For a nondivergent flow, velocity components can be written with the aid of a streamfunction:

$$[\bar{\mathbf{v}}] = \frac{g}{2\pi R_E \cos \phi} \frac{\partial \Psi_M}{\partial p} \tag{5.16}$$

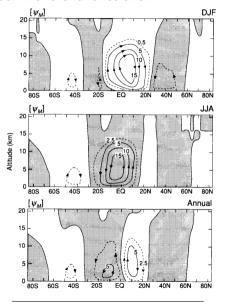
$$[\bar{\omega}] = \frac{-g}{2\pi R_E^2 \cos \phi} \frac{\partial \Psi_M}{\partial \phi}$$
 (5.17)

(5.16) and (5.17) satisfy (5.15); normalization, including the minus sign, is convention – but the relative minus sign is required. To calculate  $\Psi_M$ , first impose boundary condition  $\Psi_M=0$  at TOA, then integrate (5.16):

$$\Psi_{M} = \frac{2\pi R_{E}\cos\phi}{g} \int_{0}^{p} [\bar{\mathbf{v}}] dp'$$
 (5.18)

The normalization is chosen to give units of kg s<sup>-1</sup> (mass streamfunction); the  $\cos \phi$  factor is required to ensure constant  $\Psi_M$  for constant meridional flow. Mass transport is tangent to contours of the streamfunction. Mass flow between two contours is equal to  $\Delta \Psi_M$ .

#### Mean meridional circulation



- Hadley cell with rising branch in the ITCZ and descending in the subtropics
- ► Transport is from winter hemisphere to summer hemisphere at the surface, summer hemisphere to winter hemisphere at altitude → transport of potential energy, latent heat, sensible heat
- Mass transport by mean circulation is small outside the Hadley cell
- This is where (temporal and zonal) fluctuations in the circulation are important – eddy transport



### Averaging operators

Temporal mean

$$\overline{A} = \overline{A}(\lambda, \phi, p) = \frac{1}{\tau} \int_{-\tau/2}^{\tau/2} A(\lambda, \phi, p, t) dt$$
 (5.19)

and the zonal mean

$$[A] = [A](\phi, p, t) = \frac{1}{2\pi} \int_0^{2\pi} A(\lambda, \phi, p, t) d\lambda$$
 (5.20)

The instantaneous value of A is given by

$$A = \overline{A} + A' \tag{5.21}$$

where A' is called the *fluctuating* component of A. Likewise

$$A = [A] + A^* (5.22)$$

where  $A^*$  is the departure from the zonal mean.

Decomposition of a field into time-average and fluctuating, zonally symmetric and zonally asymmetric components:

$$A = [\bar{A}] + [A'] + \bar{A}^* + A'^* \tag{5.23}$$

# Decomposition of the flow

Products of fields contain covariance terms (where fluctuations do not average to zero)

$$\overline{AB} = \overline{A}\overline{B} + \overline{A'B'} \tag{5.24}$$

$$[AB] = [A][B] + [A^*B^*]$$
 (5.25)

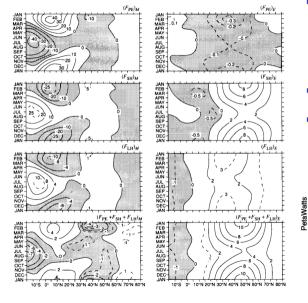
$$\left[\overline{AB}\right] = \left[\overline{A}\right] \left[\overline{B}\right] + \left[\overline{A}^*\overline{B}^*\right] + \left[\overline{A'B'}\right] \tag{5.26}$$

The terms in (5.26) are the mean circulation, stationary eddies, and transient eddies. To take a concrete example, the decomposition of northward flux of sensible heat is

$$c_{\rho}\left[\overline{vT}\right] = c_{\rho}\left[\overline{v}\right]\left[\overline{T}\right] + c_{\rho}\left[\overline{v}^*\overline{T}^*\right] + c_{\rho}\left[\overline{v'T'}\right]$$
(5.27)

This week's homework will analyze the relative importance of each contribution as a function of latitude.

### Meridional energy transport



 Recall static energy (2.61): sum of potential energy (PE), sensible heat (SH) and latent heat (LH)

$$h = gz + c_pT + L_{lv}q (5.28)$$

The divergence of poleward transport of these energy terms balances the atmospheric energy budget.

- Mean transport dominates in the Hadley cell but note large terms of opposite signs
- Eddy transport, especially in winter (large temperature gradient), dominates in midlatitudes

