Modul 04-006-1001:

WiSe 2023-2024

Formale Grundlagen (Logik)

Excercises 1

Excercise 1: Identifying sets

Which of the following are valid sets, and which are not?

- (1) a. {魚, 豐, 啟, 萬, ②}
 - b. {Obama, 'Obama', {Obama}}
 - c. $\{x \mid x \text{ is a multiple of } 17\}$
 - d. $\{x, sofa, prime, Pizza, 0, \Phi, \langle \hat{D}, x \}$
 - e. $\{\{\{\{\{\{\Phi\}\}\}\}\}\}\}$
 - f. $\{\}$ (also written as \emptyset)

Excercise 2: Identifying set members and sets

- What are the members of the following sets?
- (2) a. $\{x \mid x \text{ is a multiple of } 12 \text{ below } 60\}$
 - b. $\{x \mid x \text{ is the set containing all multiples of } 12 \text{ below } 60\}$
 - c. {vowel, yellow, 'gelb', {vowel, yellow, 'gelb'}, Φ }
 - d. $\{\{\{\{\{\{\Phi\}\}\}\}\}\}\}$
 - e. {Bart}
 - f. {Bart, 'Bart', {Bart}}
 - For the set OS = {Olaf Scholz}, which of the following is True or False?
- (3) a. Olaf Scholz is a member of OS.
 - b. {Olaf Scholz} is a member of OS.
 - c. The current Bundeskanzler of Germany is a member of OS.
 - What is the set whose only member is {S}?

Excercise 3: List to predicate notation

- Convert each of the sets in list notation below to predicate notation.
- (4) a. $\{2, 4, 6, 8, 10\}$
 - b. {Bart, Lisa, Homer, Marge, Maggie}
 - c. {Leipzig}
 - d. {'Bart', 'Lisa', 'Homer', 'Marge', 'Maggie'}
 - e. {}

Excercise 4: Predicate to list notation

- Convert each of the sets in predicate notation below to list notation.
- (5) a. $\{x \mid x \text{ is an odd number smaller than } 12\}$
 - b. $\{z \mid z \text{ is the name of the first president of the USA}\}$
 - c. {a | a is a triangular circle}

Excercise 5: Subset superset relations

• List the proper subset and proper superset relations that hold between the following sets. (To answer this question, you might first need to find out what the facts are.)

- $A = \{ x \mid x \text{ is a Beatles song written by Paul McCartney} \}$ $C = \{ x \mid x \text{ is a Beatles song written by Ringo Starr} \}$ $D = \{ \text{Let it be, Maxwell's Silver Hammer, Hey Jude} \}$ (6)

 - d. $F = \{\}$